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## Teaching Firmware as a Bridge Between Hardware and Software

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**Abstract**—The Electrical Engineering Department of the Swiss Federal Institute of Technology in Lausanne, Switzerland, has recently introduced a new course for freshmen aimed to tie together both sides of computer science (hardware, such as logic and digital systems, and software, such as classic procedural PASCAL programming), to emphasize systematic and invariant methods rather than describing rapidly changing technologies and to give a faster and stronger introduction to the profession.

This one-year course (with labs) is called an *Introduction to firmware theory*, the term firmware being comprehended as the art and the technique of transforming hardware (logic systems) into software (programs) and vice versa; the entire course is based on the central idea of equivalence between hardware and software which is exhibited by means of one preferred representation, *the binary decision tree*. In this paper, a very simple example is used to show the definition of a binary decision tree, its simplification and its decomposition. Hardware implementation is illustrated by a demultiplexer network, while software implementation is highlighted by the use of two structured languages: a high-level language called MICROPASCAL and a low-level language called L4, the latter being obtained by a compilation of the former. The conclusion gives a summary of the course, including laboratory sessions, as it is taught at present.

### I. INTRODUCTION

A number of American institutions (Drexel University in Philadelphia, Rose-Hulman Institute of Technology in Terre Haute, Indiana, and Texas A & M University) are trying experiments for restructuring their curricula for freshmen and sophomores and are searching for a “magic ingredient” that could give engineering instructors the incentive to design, develop, and test innovative approaches to undergraduate education [1].

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In the particular area of computer science, the Electrical Engineering Department of the Swiss Federal Institute of Technology in Lausanne, Switzerland has faced the same challenge and has decided to introduce in 1988 a new course for freshmen (first year) aimed to:

- give a faster and stronger introduction to the profession;
- tie together both sides of computer science: hardware (logic and digital systems) and software (classic procedural programming such as PASCAL); and
- emphasize systematic and (almost) invariant methods rather than describing fast changing present technologies.

The solution arrived at consists of a one-year course (with laboratory experiments) dedicated to an *Introduction to firmware theory*, the term firmware being comprehended as **the art and the technique of transforming hardware (logic systems) into software (programs) and vice versa**.

The entire course is therefore based on the central idea of equivalence between hardware and software; and this equivalence, which at the mathematical level rests on the concept of the algorithm, is exhibited by means of one preferred representation, *the binary decision tree*. In this paper, a very simple example (a decoder designed for an electronic watch) is used to show the definition of a binary decision tree, its simplification (Section II) and its decomposition (Section III). Hardware implementation is illustrated by a demultiplexer network (Section IV), while software implementation is highlighted by the use of two structured languages: a high-level language called MICROPASCAL and a low-level language called L4 (Section V). The conclusion gives a summary of the course, as it is taught at present at the Swiss Federal Institute of Technology.

II. SIMPLIFICATION OF BINARY DECISION TREES

A. Example: A Watch Decoder

Any combinational logic system with  $n$  input binary variables can be represented by various modes of representation: a truth table with  $2^n$  rows, a Karnaugh map of  $2^n$  cells, a binary decision tree with  $2^n$  branches.

Consider, for example, the decoder which has to detect, in an electronic watch, the number of days in a month. The months are represented by BCD (binary coded decimal) numbers in the range 1–12 (from January to December) with the aid of the following logical variables:

- $M_4$  for the tens (0 or 1);
- $M_3, M_2, M_1, M_0$  for the units (0000 ... 1001).

These are to be the inputs to a combinational system whose discrete output  $Z$  is 30, 31 or  $F$  for February. The five variables  $M_4 \dots M_0$  define  $2^5 = 32$  possible input states, 12 of which are defined and 20 being undefined or "don't care conditions" ( $\Phi$ ) for  $Z$ . The output function  $Z$  can therefore be represented by a 32-branch binary decision tree.

We will show how it is possible to use the Karnaugh map in order to simplify the original (or canonical) 32-branch binary decision tree. This process is called the *simplification of the binary decision tree*, i.e., the search of a tree with a minimal number of branches for representing a given function  $Z$ .

B. Simplifying a Binary Decision Tree

We propose the following graphical method:

- In the Karnaugh map, an output state ( $Z = 30, 31$  or  $F$ ) is entered into each of the 12 cells corresponding to the 12 input states  $M_4, M_3, M_2, M_1, M_0$  given by the specification.
- Don't care conditions ( $Z = \Phi$ ) are entered into the 20 remaining cells.
- The map is divided into *blocks* (i.e., rectangular or square groups of  $2^j$  cells with  $j = 0, 1, \dots, 5$ ), and the set of blocks must satisfy the conditions of *coverage, separability, and compatibility*. Coverage means that every cell must be included in a block. Separability means that all the cells in the same block must have the same output state, and that each cell may be included in only one block. Compatibility means that a branch variable can cut the Karnaugh map into two half-maps without cutting any block in the map, and each half-map can be likewise divided again, and so on until one obtains the set of isolated blocks. For example, in Fig. 1, the branch variables capable of starting this subdividing, i.e., the first-branch variables, are  $M_4$  or  $M_0$ .
- The set containing the fewest blocks is the *minimal set*. Each minimal set produces a minimal binary decision tree, and each block of this set (a product of the branch variables) produces one branch of the tree.

In the example of Fig. 1, one can verify the following:

- The map of 32 cells is completely covered by 7 blocks (coverage).
- The cells in each of the 7 blocks have the same output state (30, 31 or  $F$ ), and each of the 32 cells is covered

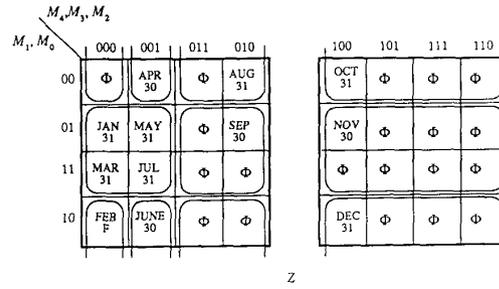


Fig. 1. Karnaugh map for the watch decoder: partition in 7 blocks.

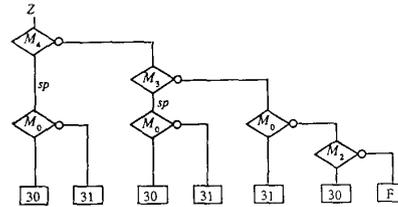


Fig. 2. Binary decision tree after simplification (7 branches).

by one block only (separability); a don't care condition ( $\Phi$ ) can be given the value 30, 31 or  $F$ .

- The first-branch variable is  $M_4$  since  $M_4$  divides the map into two half-maps of 16 cells each without cutting any block. This process can be continued with variable  $M_0$  (for  $M_4 = 1$ ) and  $M_3$  (for  $M_4 = 0$ ), and so on (compatibility).
- It is impossible to find a set with fewer than 7 blocks: therefore, the set is minimal.

Fig. 2 show a minimal binary decision tree consisting of 7 branches and realizing the given function  $Z$ : each block in the Karnaugh map is a branch of the tree. A binary decision tree has always as many *output elements*, represented by rectangles, as branches (7 in Fig. 2) and as many *test elements*, represented by diamonds, as branches minus 1 (6 in Fig. 2).

Systematic methods, similar to the classical McCluskey's minimization process, must be used to prove that this tree is truly minimal. Unfortunately, these methods are tedious to handle by hand calculation and therefore need automatic computation [2].

III. DECOMPOSITION OF BINARY DECISION TREES

A. Main Tree and Subtrees

Looking at the tree of Fig. 2, we can see two identical subtrees *sp*; the binary decision tree of Fig. 2 is therefore equivalent to the two partial trees of Fig. 3. We have thus effected a *decomposition* of the original tree into a *main tree* ( $Z = pp$ ) and a *subtree* (*sp*); the decomposition has necessitated a third type of graphical element, represented by *sp* in a rectangle with four vertical bars (Fig. 3): this is the *call of subtree element*. The decomposition of a given binary decision tree into several subtrees is equivalent to the calculation of a *binary decision diagram*, which can be viewed as a tree with reconvergent branches (Fig. 4).



*B. Other Hardware Applications*

Any sequential system can be described by a state table, in which the next state  $Y^+$  and the output state  $Z$  are functions of the input state  $X$  and the present state  $Y$ . Implementing a sequential system is therefore reduced to finding a minimal binary tree (or diagram) of the discrete function  $Y^+, Z$  which depends on the  $X$  and  $Y$  variables. The main problem remains the simplification and the possible decomposition of the canonical tree. An example of a reversible counter is detailed in [5] and [20], while an exhaustive study of finite state machines can be found in [20]. A general method for synthesizing hardware systems by means of binary decision trees can be summarized as follows: starting with a Karnaugh map (for combinational systems) or with a state table (sequential systems), simplification and/or decomposition produces a tree with or without reconvergent branches, representing a discrete function  $Z$  equivalent to  $n$  boolean functions  $Z_n, Z_{n-1}, \dots, Z_1$ . One single demultiplexer tree with OR gates (and, in the case of a sequential circuit, with flip-flops) implements the original specification; it can be shown that a network with  $n$  multiplexer trees (with flip-flops in the case of a sequential circuit) can constitute an equivalent system [20].

In conclusion, the method of binary decision trees and diagrams can easily and regularly be used in all hardware designs. The only limitation for hand calculation, due to the use of Karnaugh maps, is the number of input variables.

V. SOFTWARE IMPLEMENTATION

*A. Structured Programming*

The main advantage of a decomposition of a tree into a main tree and several subtrees is that this preserves the structure of trees which, in contrast to decision diagrams with convergent branches, meet the requirements of structured programming.

Let us remember the definition of a *structured program*:

- a) the *output instruction do s*, characterized by an action  $s$  and having one input terminal connected to the preceding instruction and one output terminal connected to the next instruction, is a structured program. If  $P$  and  $Q$  are structured programs then
- b) the *sequence of P and Q (do PQ)* is a structured program;
- c) the *iteration of P (while a do P)* is a structured program;
- d) the *test giving P or Q (if a then P else Q)* is a structured program; and
- e) all existing structured programs are those which can be obtained by applying definitions a) through d) a finite number of times.

- a) **DO**  $s$  **GO TO**  $ADR+1$
- b) **IF**  $a$  **THEN**  $ADR+1$  **ELSE**  $ADR0$   
with the special case when  $a = 0$ : **GO TO**  $ADR0$
- c) **CALL**  $ADSP$  **RET TO**  $ADR+1$
- d) **RET**

- (action);
- (test),
- (unconditional jump);
- (procedure call);
- (return from procedure)

MICROPASCAL	ADR	L4
<b>program pp</b>	-	<b>PROGRAM pp</b>
<b>if M4</b>	00	<b>IF M4 ELSE 03</b>
<b>call sp</b>	01	<b>CALL 10</b>
<b>else</b>	02	<b>GO TO 0D</b>
<b>if M3</b>	03	<b>IF M3 ELSE 06</b>
<b>call sp</b>	04	<b>CALL 10</b>
<b>else</b>	05	<b>GO TO 0D</b>
<b>if M0</b>	06	<b>IF M0 ELSE 09</b>
<b>do 31</b>	07	<b>DO 31</b>
<b>else</b>	08	<b>GO TO 0D</b>
<b>if M2</b>	09	<b>IF M2 ELSE 0C</b>
<b>do 30</b>	0A	<b>DO 30</b>
<b>else</b>	0B	<b>GO TO 0D</b>
<b>do F</b>	0C	<b>DO F</b>
<b>endif</b>	-	<b>ENDIF</b>
<b>procedure sp</b>	-	<b>PROCEDURE sp</b>
<b>if M0</b>	10	<b>IF M0 ELSE 13</b>
<b>do 30</b>	11	<b>DO 30</b>
<b>else</b>	12	<b>GO TO 14</b>
<b>do 31</b>	13	<b>DO 31</b>
<b>endif</b>	-	<b>ENDIF</b>
<b>end procedure</b>	14	<b>RET</b>
<b>end program</b>	-	<b>END PROGRAM</b>

Fig. 7. Software implementation in MICROPASCAL and L4 structured languages (ADR: present address).

*B. Structuring and Interpreting Binary Decision Trees*

Binary decision trees, unlike decision diagrams, can be directly implemented in a structured program (Fig. 7). This program, first expressed in a high-level language called MICROPASCAL, a minimal subset of PASCAL [5], is derived from the decomposition of trees (Fig. 3) as follows:

- the main tree is implemented as the main program  $pp$ , beginning with the keyword **program** ... and terminating with **end program**;
- the subtree  $sp$  is realized as a single procedure  $sp$ , starting with the keyword **procedure** ... and terminating with **end procedure**;
- each test element of the trees (a diamond in Fig. 3) is implemented as an **if...else...endif** structure;
- each output element (a rectangle) is implemented as a **do...** instruction, while each call of subtree element (a rectangle with four vertical bars) is implemented as a **call...** instruction.

A straightforward compilation, by hand or by computer, transforms the MICROPASCAL program in an equivalent low-level language L4 program (Fig. 7). This language is also structured, and is implemented by a set of four instructions only:

where *ADR* is the actual address, *ADRO* and *ADSP* next addresses. The keywords **PROGRAM...**, **ENDIF**, **PROCEDURE...** and **END PROGRAM** are merely comments, without any address.

If the decomposition of binary trees is minimal (i.e., has a minimal number of test elements), then the high-level language MICROPASCAL program and the low-level language **L4** program will be minimal too, i.e., will have a minimal number of test structures (**if...else..endif** or **IF...ELSE...GO TO...ENDIF**).

The **L4** program of Fig. 7 can be directly interpreted by a simple sequential machine, a *binary decision machine*, which has been described elsewhere [5]; this machine is built from classical bit-slice integrated circuits (*controller* or *sequencer*) or directly obtained as a single circuit with an UV-erasable and reprogrammable memory (for example: CMOS field-programmable controller from Advanced Micro Devices).

## VI. CONCLUSION

### A. Advantages and Drawbacks

The main advantage of the proposed approach is its universality: minimizing binary decision trees or diagrams produces minimal hardware circuits (i.e., multiplexer or demultiplexer networks with a minimal number of components) or minimal program (i.e., programs with a minimal number of **IF...THEN...ELSE...** instructions); this approach is a powerful tool for designing both hardware and software.

On the hardware side, the increasing use of field programmable gate arrays (FPGA) based upon one- or two-variable multiplexer (e.g., the ACTEL family) makes our approach particularly attractive; the only drawback is the delay: in the worst case (a branch of the tree without any simplification), the signal must go through  $n$  circuits (multiplexer or demultiplexer) for  $n$  input variables, instead of the two levels for classical AND-OR networks.

On the software side, the use of binary decision machines built from actual integrated circuits becomes more and more popular for the design of real time and medium scale programs (approx. 500 instructions). The binary decision tree/diagram is a tool for obtaining shorter programs and for introducing a true methodology in software design.

### B. Organization of the Course

The first part of the new course *Introduction to firmware theory* is quite standard: it is devoted to the classical switching theory and to the analysis and synthesis of logic systems, both combinational and sequential (11 sessions of four hours each, whose one is dedicated to the lecture, the three other being devoted to laboratory experiments).

The second part, which is the subject of this paper, comprises seven sessions of four hours each (one hour of lecture and three hours of laboratory) as follows:

#### 1) Memories:

- Definition and functional analysis of ROM and RAM;
- RAM with 3-state circuits and bi-directional buses;
- Realization of a classical state machine with RAM.

#### 2) Binary Decision Trees:

- Definition, simplification, and decomposition of binary trees using Karnaugh map;
- Hardware implementation: demultiplexer/multiplexer network;
- Software implementation: definition of language **L1** consisting of two types of instructions {**IF a THEN ADR1 ELSE ADR0**} and {**DOs GO TO ADR+**};
- Interpretation of language **L1** by means of a hardware interpreter: a binary decision machine;
- Application: comparator of two 4-bit numbers.

#### 3) Subprograms, Procedures, and Stack Machine:

- Definition of subprograms, procedures, and nested procedures;
- Software implementation of procedures: language **L2** with four types of instructions {**IF a THEN ADR1 ELSE ADR0, DO s GO TO ADR+, CALL ADSP RET TO ADR, RET**};
- Interpretation of language **L2** by a hardware interpreter: a binary decision machine with a stack;
- Procedure call with parameter passing;
- Applications: counter modulo- $n$ , decomposition of counters, iterative combinational system (an adder).

#### 4) Incremental Programs and Controller:

- Definition of incremental programs;
- Software implementation with a modified version of language **L2**: **L3 = {IF a THEN ADR+1 ELSE ADR0, DO s GO TO ADR+1, CALL ADSP GO TO ADR+1, RET}**;
- Interpretation of **L3** by a stack machine built of an industrial controller;
- Application: digital clock.

#### 5) Structured Programming:

- Definition of the four constructions of structure programming;
- Syntactic definition of two structured languages: a high-level language MICROPASCAL with 11 instruction types, a low-level language **L4**, which is equivalent to **L3** augmented of several keywords;
- Realization of a classical state table with minimal coding: software implementation based on a single tree and described by a structured MICROPASCAL or **L4** program;
- Realization of a classical state table with one-out-of- $n$  coding: software implementation based on  $n$  trees (one tree for each state) and described by a unstructured **L3** program;
- Applications: reversible counter, car starter;
- Conclusion: methods for structuring unstructured programs.

#### 6) Top-Down Programming:

- Method of successive refinements;
- Case study: the clock algorithm, for a complex digital watch;

- First implementation with a complex program and a simple processing unit (software dominant solution);
- Second implementation with a simple program and a complex processing unit (hardware dominant solution).

#### 7) Microprogramming a Universal Processor:

- Analysis of an arithmetical and logic unit with registers (RALU);
- Getting a universal processor by the assemblage of a binary decision machine with a stack (control unit) and a RALU (processing unit);
- Case study: microprogramming the multiplication of two binary numbers;
- Further application (for advanced students): microprogramming the compilation of MICROPASCAL high-level language into L4 low-level language.

Our course is followed in the three next years by more specialized lectures on hardware (microprocessors, computer architecture, etc.); it must be pointed out that students are taught during the first year a classical course about procedural programming (PASCAL) during 15 sessions of three hours each and based upon reference [21].

#### C. Related Works

Binary decision trees have become more and more popular, especially for analyzing and testing logic circuits [6]–[8]. Programming a binary decision machine and using it to replace hardwired logic systems or classical microprocessors is less popular; nevertheless, after the historical publications of Lee [9], Clare [10] and Boute [11], a number of researchers in the United States and overseas have paid great attention to this new methodology and/or have realized VLSI binary decision machines:

- W. I. Fletcher, Utah State University, Logan [12] (pp. 600–645);
- M. Andrews, Colorado State University [13] (pp. 210–274);
- P. J. A. Zsombor-Murray *et al.*, McGill University, Montreal, Canada [14];
- M. Davio *et al.*, Philips Research Laboratory, Brussels and Université Catholique de Louvain, Belgium [15];
- L. D. Coraor *et al.*, Pennsylvania State University, University Park [16];
- A. Ginetti, C. Trullemans, Université Catholique de Louvain, Belgium [17];
- C. Piguët, Centre suisse d'électronique et de microtechnique, Neuchâtel, Switzerland [18].

The course described in this paper is based on the book [19], in French, which was recently published in English [20]; significant extracts of the latter can be found in [5].

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