

# Digital Design

## Chapter 1: Introduction

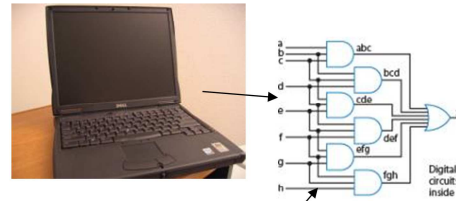
Slides to accompany the textbook *Digital Design*, First Edition,  
by Frank Vahid, John Wiley and Sons Publishers, 2007.  
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## Why Study Digital Design?

- Look “under the hood” of computers
  - Solid understanding --> confidence, insight, even better programmer when aware of hardware resource issues
  
- Electronic devices becoming digital
  - Enabled by shrinking and more capable chips
  - Enables:
    - Better devices: Better sound recorders, cameras, cars, cell phones, medical devices,...
    - New devices: Video games, PDAs, ...
  - Known as “embedded systems”
    - Thousands of new devices every year
    - Designers needed: Potential career direction



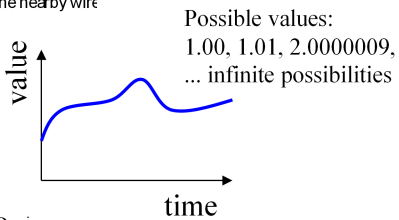
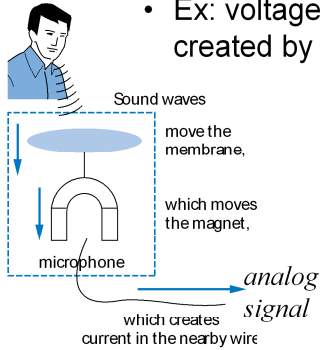
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## What Does "Digital" Mean?

- Analog signal

- Infinite possible values

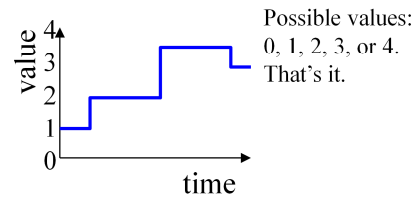
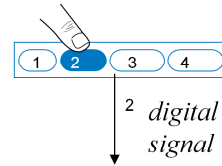
- Ex: voltage on a wire created by microphone



- Digital signal

- Finite possible values

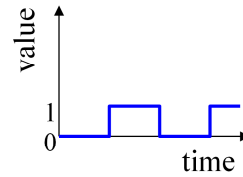
- Ex: button pressed on a keypad



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## Digital Signals with Only Two Values: Binary

- **Binary** digital signal -- only *two* possible values
  - Typically represented as **0** and **1**
  - One *binary digit* is a **bit**
  - We'll only consider *binary* digital signals
  - Binary is popular because
    - Transistors, the basic digital electric component, operate using *two* voltages (more in Chpt. 2)
    - Storing/transmitting one of *two* values is easier than three or more (e.g., loud beep or quiet beep, reflection or no reflection)



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# Example of Digitization Benefit

- Analog signal (e.g., audio) may lose quality
  - Voltage levels not saved/copied/transmitted perfectly
- Digitized version enables near-perfect save/cpy/trn.
  - "Sample" voltage at particular rate, save sample using bit encoding
  - Voltage levels still not kept perfectly
  - But we can distinguish 0s from 1s

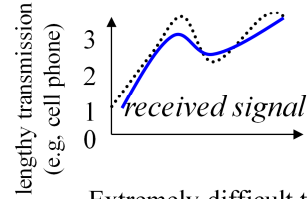
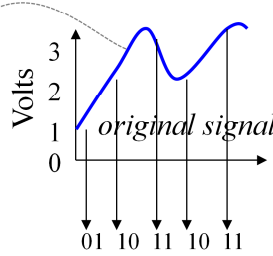
Let bit encoding be:

- 1 V: "01"
- 2 V: "10"
- 3 V: "11"

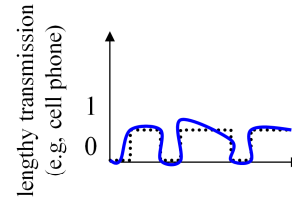
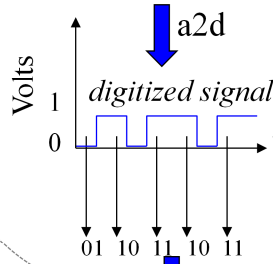
*Digitized signal not perfect re-creation, but higher sampling rate and more bits per encoding brings closer.*



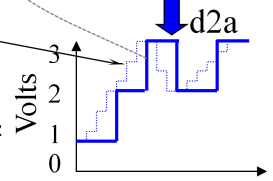
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Extremely difficult to fix



Can fix -- easily distinguish 0s and 1s, restore



same

## Digitized Audio: Compression Benefit

- Digitized audio can be compressed
  - e.g., MP3s
  - A CD can hold about 20 songs uncompressed, but about 200 compressed
- Compression also done on digitized pictures (jpeg), movies (mpeg), and more
- Digitization has many other benefits too

Example compression scheme:

00 --> 0000000000

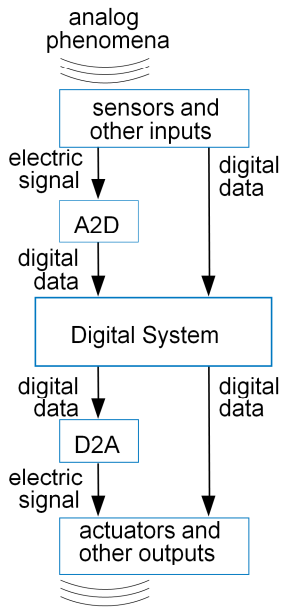
01 --> 1111111111

1X --> X

0000000000 0000000000 0000001111 1111111111  
                  ↓          ↓          ↓          ↓  
                  00 00 10000001111 01

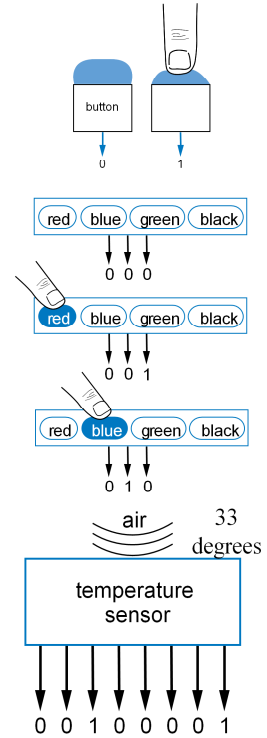


# How Do We Encode Data as Binary for Our Digital System?



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- Some inputs inherently binary
  - Button: not pressed (0), pressed (1)
- Some inputs inherently digital
  - Just need encoding in binary
  - e.g., multi-button input: encode red=001, blue=010, ...
- Some inputs analog
  - Need analog-to-digital conversion
  - As done in earlier slide -- sample and encode with bits



## How to Encode Text: ASCII, Unicode

- ASCII: 7- (or 8-) bit encoding of each letter, number, or symbol
- Unicode: Increasingly popular 16-bit bit encoding
  - Encodes characters from various world languages

Symbol	Encoding	Symbol	Encoding
R	1010010	r	1110010
S	1010011	s	1110011
T	1010100	t	1110100
L	1001100	l	1101100
N	1001110	n	1101110
E	1000101	e	1100101
0	0110000	9	0111001
.	0101110	!	0100001
<tab>	0001001	<space>	0100000

**Question:**  
What does this ASCII bit sequence represent?

1010010 1000101 1010011 1010100

REST

- <http://www.asciitable.com>



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Note: small red "a" (a) in a slide indicates animation ← 8

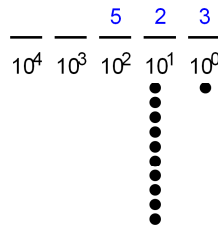


# How to Encode Numbers: Binary Numbers

- Each position represents a quantity; symbol in position means how many of that quantity

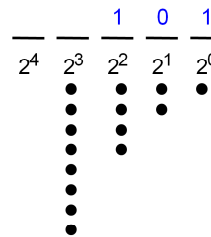
- Base ten (*decimal*)

- Ten symbols: 0, 1, 2, ..., 8, and 9
- More than 9 -- next position
  - So each position power of 10
- Nothing special about base 10 -- used because we have 10 fingers

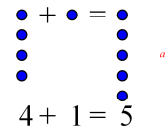


- Base two (*binary*)

- Two symbols: 0 and 1
- More than 1 -- next position
  - So each position power of 2



Q: How much?



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# How to Encode Numbers: Binary Numbers

- Working with binary numbers

- In base ten, helps to know powers of 10

- one, ten, hundred, thousand, ten thousand, ...

- In base two, helps to know powers of 2

- one, two, four, eight, sixteen, thirty two, sixty four, one hundred twenty eight

- (Note: unlike base ten, we don't have common names, like "thousand," for each position in base ten -- so we use the base ten name)

- Q: count up by powers of two

$2^9$	$2^8$	$2^7$	$2^6$	$2^5$	$2^4$	$2^3$	$2^2$	$2^1$	$2^0$
512	256	128	64	32	16	8	4	2	1

512 256 128 64 32 16 8 4 2 1 .



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# Converting from Decimal to Binary Numbers: Subtraction Method (Easy for Humans)

- Get the binary weights to add up to the decimal quantity
  - Work from left to right
  - (Right to left – may fill in 1s that shouldn't have been there – try it).
- To make the job easier (especially for big numbers), we can just subtract a selected binary weight from the (remaining) quantity
  - Then, we have a new remaining quantity, and we start again (from the present binary position)
  - Stop when remaining quantity is 0

Desired decimal number: **17**

$$\begin{array}{r} \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \\ 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \\ \underline{0} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \\ 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array} = 32$$

too much

$$\begin{array}{r} \underline{\quad} \quad \underline{1} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \quad \underline{\quad} \\ 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array} = 16 \quad (17-16=1)$$

ok, keep going

$$\begin{array}{r} \underline{\quad} \quad \underline{1} \quad \underline{0} \quad \underline{0} \quad \underline{0} \quad \underline{\quad} \\ 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array} = 8, 4, 2$$

too much

$$\begin{array}{r} \underline{\quad} \quad \underline{0} \quad \underline{1} \quad \underline{0} \quad \underline{0} \quad \underline{1} \\ 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array} = 1-1=0$$

DONE

$$\begin{array}{r} \underline{\quad} \quad \underline{1} \quad \underline{0} \quad \underline{0} \quad \underline{0} \quad \underline{1} \\ 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array} \quad \text{answer}$$



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## Converting from Decimal to Binary Numbers: Subtraction Method Example

- Q: Convert the number "29" from decimal to binary

A: Remaining quantity

29

Binary Number

$\frac{0}{32} \frac{0}{16} \frac{0}{8} \frac{0}{4} \frac{0}{2} \frac{0}{1}$

$\frac{29}{-16}$   
13

$\frac{0}{32} \frac{1}{16} \frac{0}{8} \frac{0}{4} \frac{0}{2} \frac{0}{1}$

$\frac{13}{-8}$   
5

$\frac{0}{32} \frac{1}{16} \frac{1}{8} \frac{0}{4} \frac{0}{2} \frac{0}{1}$   
*8 is more than 7, can't use*

$\frac{5}{-4}$   
1

$\frac{0}{32} \frac{1}{16} \frac{1}{8} \frac{1}{4} \frac{0}{2} \frac{0}{1}$

$\frac{1}{-1}$   
0

$\frac{0}{32} \frac{1}{16} \frac{1}{8} \frac{1}{4} \frac{0}{2} \frac{1}{1}$

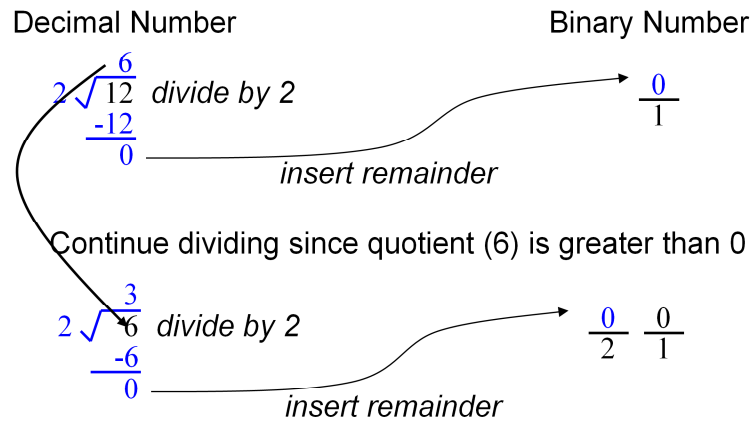
Done! 29 in decimal is 10111 in binary.



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## Converting from Decimal to Binary Numbers: Division Method (Good for Computers)

- Divide decimal number by 2 and insert remainder into new binary number.
  - Continue dividing quotient by 2 until the quotient is 0.
- Example: Convert decimal number 12 to binary



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Continue dividing since quotient (3) is greater than 0

## Converting from Decimal to Binary Numbers: Division Method (Good for Computers)

- Example: Convert decimal number 12 to binary (continued)

Decimal Number	Binary Number
$  \begin{array}{r}  2 \overline{) 12} \\  \underline{-2} \\  0  \end{array}  $	$  \begin{array}{r}  \frac{1}{4} \quad \frac{0}{2} \quad \frac{0}{1}  \end{array}  $
<p><i>insert remainder</i></p>	

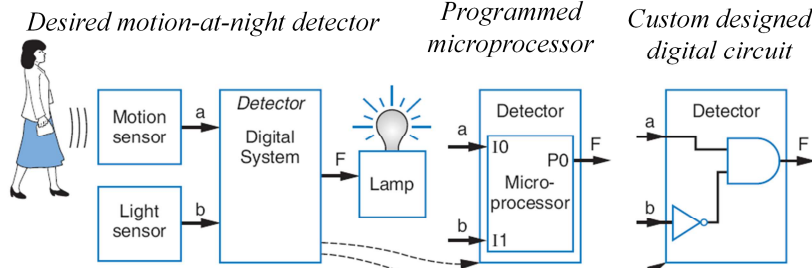
Continue dividing since quotient (1) is greater than 0

$  \begin{array}{r}  2 \overline{) 6} \\  \underline{-0} \\  6  \end{array}  $	$  \begin{array}{r}  \frac{1}{8} \quad \frac{1}{4} \quad \frac{0}{2} \quad \frac{0}{1}  \end{array}  $
<p><i>insert remainder</i></p>	

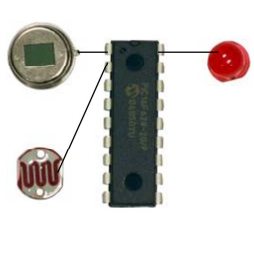
Since quotient is 0, we can conclude that 12 is 1100 in binary



# Implementing Digital Systems: Programming Microprocessors Vs. Designing Digital Circuits



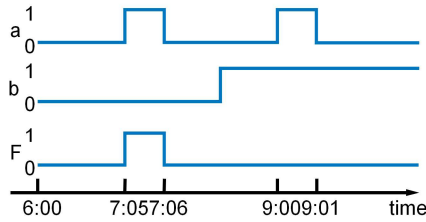
- Microprocessors a common choice to implement a digital system
  - Easy to program
  - Cheap (as low as \$1)
  - Available now



10	P0
11	P1
12	P2
13	P3
14	P4
15	P5
16	P6
17	P7

```

void main()
{
  while (1) {
    P0 = I0 && !I1;
    // F = a and !b,
  }
}
    
```





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# Digital Design: When Microprocessors Aren't Good Enough

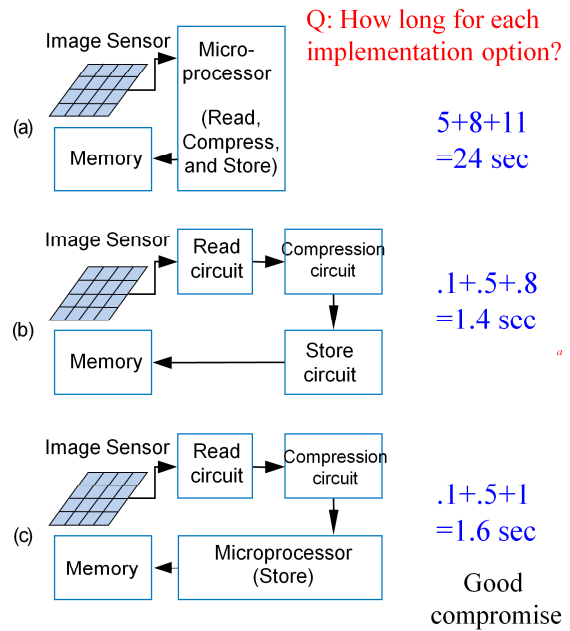
- With microprocessors so easy, cheap, and available, why design a digital circuit?
  - Microprocessor may be too slow
  - Or too big, power hungry, or costly

Sample digital camera task execution times (in seconds) on a microprocessor versus a digital circuit:

Task	Microprocessor	Custom Digital Circuit
Read	5	0.1
Compress	8	0.5
Store	1	0.8



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## Chapter Summary

- Digital systems surround us
  - Inside computers
  - Inside huge variety of other electronic devices (embedded systems)
- Digital systems use 0s and 1s
  - Encoding analog signals to digital can provide many benefits
    - e.g., audio -- higher-quality storage/transmission, compression, etc.
  - Encoding integers as 0s and 1s: Binary numbers
- Microprocessors (themselves digital) can implement many digital systems easily and inexpensively
  - But often not good enough -- need custom digital circuits

