

ITCS 4111/5111: Intro to Natural Language Processing

Coreference Resolution

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Coreference Resolution: Wikipedia text

- Determine which noun phrases (**mentions**) refer to the same discourse **entity**.

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CoreferenceResolution: Mathematical Statements

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Application: Social Networks from Text

- Input = a large text, such as a novel or a play, for example *Romeo and Juliet*, which contains a number of characters, e.g. **Romeo Montague**, **Juliet Capulet**, **Mercutio**, **Benvolio**.
- Output = a social network extracted from the text:
 - Each character is associated a node, and edges between two nodes are created for interactions between those two characters that are explicitly expressed in sentences.
 - Each edge is labeled with the type of interaction:
 - For example *Romeo talked to Juliet* would lead to the creation of an edge between **Romeo Montague** and **Juliet Capulet** that is labeled with *talked to*.
- Your solution will be graded based on its precision (how accurate it is) and recall (how many such interactions it correctly extracts).
 - Given that NLP tools are often less than 100\% accurate, elaborate on how you could increase the quality of the extracted social network.

Application: Social Networks from Text

- Pipeline of NLP tasks:
 1. Tokenization and sentence segmentation.
 2. Syntactic parsing.
 - POS tagging to identify pronouns.
 3. Named entity recognition.
 4. Coreference resolution.

Show pipeline processing on the following example:

Romeo was walking his dog when he met Mercutio's neighbor, Juliet. She asked him if the dog was a golden retriever.

Coreference using SpaCy

- **SpaCy** uses the NeuralCoref model, as implemented by **Huggin Face**:
 - <https://spacy.io/universe/project/neuralcoref>
 - <https://github.com/huggingface/neuralcoref>
- Currently not working in version 3 with Python 3.8, need version 2 with Python 3.7:
 - `conda create --name spacy-coref`
 - `conda activate spacy-coref`
 - `conda install python=3.7`
 - `pip install spacy==2.1.0`
 - `pip install neuralcoref`
 - `pip install https://github.com/explosion/spacy-models/releases/download/en_core_web_lg-2.1.0/en_core_web_lg-2.1.0.tar.gz`
 - `conda install -c conda-forge jupyterlab # select Python 3 as kernel in Jupyter.`

Coreference using SpaCy

```
In [1]: # Load your usual SpaCy model (one of SpaCy English models)
import spacy
import en_core_web_lg

nlp = en_core_web_lg.load()

# Add neural coref to SpaCy's pipe.
import neuralcoref
neuralcoref.add_to_pipe(nlp)

# You can now use NeuralCoref as you usually manipulate a SpaCy document annotations.
doc = nlp(u'My sister has a dog. She loves him.')

doc._.has_coref
doc._.coref_clusters
```

```
Out[1]: [My sister: [My sister, She], a dog: [a dog, him]]
```

```
In [5]: doc = nlp(u'Romeo was walking his dog when he met Mercutio\'s neighbor, Juliet.')
doc._.coref_clusters
```

```
Out[5]: [Romeo: [Romeo, his, he]]
```


More recent, more accurate approaches

1. CorefQA: Coreference Resolution as Query-based Span Prediction [Wu et al., ACL'20]
 - <https://github.com/ShannonAI/CorefQA>
2. BERT for Coreference Resolution: Baselines and Analysis [Joshi et al., EMNLP'19]
 - <https://github.com/mandarjoshi90/coref>
3. Coreference Resolution with Entity Equalization [Kantor & Globerson, ACL'19]
 - <https://github.com/kkjawz/coref-ee>
4. Higher-order Coreference Resolution with Coarse-to-fine Inference [Lee et al, NAACL'18]
 - <https://github.com/kentonl/e2e-coref>
5. End-to-end Neural Coreference Resolution [Lee et al., EMNLP'17]
 - <https://github.com/kentonl/e2e-coref>

Supplementary Readings

- Stanford CS 224N slides on coreference resolution.
- Chapter 21 (Coreference Resolution) in [Jurafsky & Martin]
- Chapter 15 (Reference Resolution) in [Eisenstein]
- The papers on the previous slide.