

## ITCS 6150/8150 Project

**OPTION 1:** Implement the verification method (called RS-method), described below, of whether a given formula in the propositional calculus is a tautology.

Assume that  $L_0$  is a language of order zero (propositional calculus). Letter S (with indices) will denote finite sequences  $(\alpha_1, \alpha_2, \dots, \alpha_m)$  of formulas in  $L_0$ .

If  $S_1 = (\alpha_1, \alpha_2, \dots, \alpha_m)$  and  $S_2 = (\beta_1, \beta_2, \dots, \beta_n)$  and  $\alpha, \beta$  are any formulas then  $S_1, \alpha, S_2$  and  $S_1, \alpha, \beta, S_2$  denote sequences  $(\alpha_1, \alpha_2, \dots, \alpha_m, \alpha, \beta_1, \beta_2, \dots, \beta_n)$  and  $(\alpha_1, \alpha_2, \dots, \alpha_m, \alpha, \beta, \beta_1, \beta_2, \dots, \beta_n)$ .

A **formula** in  $L_0$  is **indecomposable** if it is either a propositional variable or negation of propositional variable.

A **sequence is indecomposable** provided it is formed only of indecomposable formulas

A **sequence is fundamental** if it simultaneously contains a formula  $\alpha$  and its negation  $\neg\alpha$ .

We consider two types of schemas:  $S_1/S_2$  and  $S_1/(S_2; S_3)$ .  $S_1$  is called is a premise and  $S_2, S_3$  conclusions. If a schema is of the form  $S_1/(S_2;S_3)$ , then  $S_2$  is left conclusion and  $S_3$  right conclusion. The following 7 schemas are considered:

$[S_1, (\alpha \cup \beta), S_2] / [S_1, \alpha, \beta, S_2]$        $[S_1, (\alpha \cap \beta), S_2] / [S_1, \alpha, S_2; S_1, \beta, S_2]$

$[S_1, \neg(\alpha \cap \beta), S_2] / [S_1, \neg\alpha, \neg\beta, S_2]$        $[S_1, \neg(\alpha \cup \beta), S_2] / [S_1, \neg\alpha, S_2; S_1, \neg\beta, S_2]$

$[S_1, (\alpha \rightarrow \beta), S_2] / [S_1, \neg\alpha, \beta, S_2]$        $[S_1, \neg(\alpha \rightarrow \beta), S_2] / [S_1, \alpha, S_2; S_1, \neg\beta, S_2]$

$[S_1, \neg\neg\alpha, S_2] / [S_1, \alpha, S_2]$ , where  $S_1$  is indecomposable in all schemas.

Let's denote by  $D(\alpha)$  the diagram (tree) built for  $\alpha$  using the above seven schemas.

**FACT:** Formula  $\alpha$  is a propositional tautology if and only if all end sequences in the diagram  $D(\alpha)$  (leaves in  $D(\alpha)$ ) are fundamental.

**System Input:** propositional formula; **System output:** yes/no

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**OPTION 2:** Write a program which solves N queens puzzle ( $8 < N < 13$ ).

**Input:** N; **Output:**  $N \times N$  Boolean array with 1's showing final position of queens.

Your program should use heuristics minimizing the search space.