Algorithm for Generalization of Action Rules to Summaries

by
Angelina A. Tzacheva

Department of Informatics, University of South Carolina Upstate
Spartanburg, SC 29303 USA.
e-mail: ATzacheva@USCUpstate.edu

Abstract: A knowledge discovery system is prone to yielding plenty of patterns, presented in the form of rules. Sifting through to identify useful and interesting patterns is a tedious and time consuming process. An important measure of interestingness is: whether or not the pattern can be used in the decision making process of a business to increase profit. Hence, actionable patterns, such as action rules, are desirable. Action rules may suggest actions to be taken based on the discovered knowledge. In this way contributing to business strategies and scientific research.

The large amounts of knowledge in the form of rules presents a challenge of identifying the essence, the most important part, of high usability. We focus on decreasing the space of action rules through generalization. In this paper, we propose an improved method for discovering short descriptions of action rules. The new algorithm produces summaries by maximizing the diversity of rule pairs, and minimizing the cost of the suggested actions.

Keywords: action rules, interestingness, actionable knowledge discovery, summaries, diversity, generalization, flexible attributes, cost of action rules

1. Introduction

Data mining, or knowledge discovery, is frequently referred to in the literature as the process of extracting interesting information or patterns from large databases. There are two major directions in data mining research: patterns and interest. The pattern discovery techniques include: classification, association, and clustering. Interest refers to the pattern applications in business, or other organizations, being useful or meaningful [1].

Since the pattern discovery techniques often generate large amounts of knowledge, they require a great deal of expert manual to post-process the mined results. Therefore, one of the central research problems in the field relates to reducing the volume of the discovered patterns, and selecting appropriate interestingness measures.

These measures are intended for selecting and ranking patterns according to their potential interest to the user. Good measures also allow the time and space costs of the mining process to be reduced. Although much work has been
conducted in this area, so far there is no widespread agreement on a formal definition of interestingness in this context. Based on the variety of definitions presented to-date, interestingness is perhaps best treated as a broad concept that emphasizes: conciseness, coverage, reliability, peculiarity, diversity, novelty, surprisingness, utility, and actionability [2].

In this work we focus on actionability and diversity.

**Actionability** - an important measure of interestingness is: how actionable the patterns are, i.e. to what extent the user can act on them to his/her advantage. For instance, whether or not the pattern can be used in the decision making process of a business to increase profit. Hence, recent research focuses on making it easier for the user to grasp the significance of the mined rules, in the context of a business action plan [1, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12].

An action rule, provides hints to a business user to what changes within flexible attributes are needed in order to re-classify customers from low profitability to high profitability class, introduced by Ras an Wieczorkowska [8]. It is assumed that attributes in a database are divided into two groups: stable and flexible. By stable we mean attributes whose values cannot be changed (age, place of birth, number of children). On the other hand, attributes (like interest rate, or loan approval) whose values can be changed or influenced are called flexible. Each action rule was originally constructed from certain pairs of classification rules. The notion of action rule was extended by Tsay and Ras in [9], and a new simplified strategy for extraction was proposed by Ras and Wyrzykowska in [5].

**Diversity** - a pattern is diverse if its elements differ significantly from each other, while a set of patterns is diverse if the patterns in the set differ significantly from each other [2]. Diversity is a common factor for measuring the interestingness of summaries [13].

**Summaries** - summarization is one of the major tasks in knowledge discovery and the key issue in online analytical processing (OLAP) systems. The essence of summarization is the formation of interesting and compact descriptions of raw data at different concept levels, which are called summaries. For example, sales information in a company may be summarized to levels of area, such as City, Province, and Country. It can also be summarized to levels of time, such as Week, Month, and Year.

According to a simple point of view, a summary can be considered diverse if its probability distribution is far from the uniform distribution. The more diverse a summary, the more interesting it is, because in the absence of any relevant knowledge, a user commonly assumes that the uniform distribution will hold in a summary. We are unaware of any existing research on using diversity to measure the interestingness of classification rules, association rules [2], or action rules.

The organization of this paper is as follows: first, we review related work that has appeared in section 2; the approach of creating action rules summaries
is presented in section 3; section 4 discusses notion of diversity; the cost and the hierarchy is described in section 5; the new algorithm for generalization of action rule summaries is in section 6; and, finally, in section 7 we conclude and make future work remarks.

2. Related Work

In the paper by Ras and Wieczorkowska [8], the notion of an action rule was introduced. The main idea was to generate, from a database, special type of rules which basically form a hint to users showing a way to re-classify objects with respect to some distinguished attribute (called a decision attribute). Values of some of attributes, used to describe objects stored in a database, can be changed and this change can be influenced and controlled by user. However, some of these changes (for instance "profit") can not be done directly to a decision attribute. In addition, the user may be unable or unwilling to proceed with the actions.

For this reason Tzacheva and Ras [6] introduce the notion of a cost and feasibility of an action rule. They suggest a heuristic strategy for creating new action rules, where objects supporting the new action rule also support the initial action rule but the cost of reclassifying them is lower or even much lower for the new rule. In this way the rules constructed are of more interest to the users.

Extended action rules, discussed in Tsay and Ras [9], form a special subclass of action rules. They construct them by extending headers of action rules in a way that their confidence is getting increased. The support of extended action rules is usually lower than the support of the corresponding action rules.

A new simplified strategy for action rule extraction was proposed by Ras and Wyrzykowska in [5]. In that work, they no longer use pairs of classification rules, but rather "grab" the objects. In this sense the action rules are mined directly from the database.

In [7] Tzacheva and Ras combine the approaches of [5], [6], and [9] leading to an improved constraint based action rule discovery with single classification rules. The minimum support, confidence, and feasibility parameters are specified by the user to produce an action rule of desirable low cost.

Yang and Cheng [12] aim for converting individuals from an undesirable class to a desirable class. The work proposes actions to switch customers to a more desirable class. It is rooted in case-base reasoning, where typical positive cases are identified to form a small and highly representative case base. This "role model" is then used to formulate marketing actions. The notion of cost of the action is also regarded. They use 1-NN classifier, 1-cluster-centroid classifier, or SVM. Such classifiers could become inadequate for disk-resident data due to their long computational time.

Ras et al.'s work on action rules is probably the pioneer in the action rule mining [5, 6, 7, 8, 9]. The notion of actionable attribute and the stable attribute
is found from the beginning of their work. In most of their methods, they use a heuristic rule discovery method first to obtain a set of rules, then they use a procedure which pairs a rule which predicts the positive class with a related rule which predicts the negative class. Unlike an exhaustive method, their method can miss important rules.

Mining action rules from scratch \([1, 5, 12]\), i.e. directly from the database without using pairs of classification rules, or a similar approach which will present an exhaustive method, would supply us with all important rules. Clearly, the space of such rules is quite huge, so a generalization technique, such as creating summaries, would provide great means for reducing the space and furnish the user with the essence of the actionable knowledge.

Tzacheva \([2]\) introduced a generalization technique, which creates summaries of action rules, by utilizing an exhaustive method. The author provided great means for reducing the space and furnished the user with the essence of the actionable knowledge. The author also introduced the notion of diversity of action rule summaries \([2]\).

In this work, we present a new algorithm for generalization of action rules. It maximizes the diversity of rule pairs, and minimizes the cost of the suggested actions.

Tzacheva \([2]\) suggested removing the high cost rules, when creating summaries, in order to additionally decrease the space of action rules. However, did not discuss how the cost will change, or how it will be computed when creating summaries. In this work, we suggest an average approach to computing the cost, which leads to cost decrease as we go up in the generalization hierarchy.

3. Summaries of Action Rules

3.1. Exhaustive Mining

In \([5]\) Ras and Wyrzykowska propose a new simplified strategy for constructing action rules as follows:

Let us assume that \(S = (U, A_{St} \cup A_{Fl} \cup \{d\})\) is a decision system, where \(d \notin A_{St} \cup A_{Fl}\) is a distinguished attribute called the decision. Assume also that \(d_1 \in V_d\), where \(V_d\) is the domain of \(d\) and \(x \in U\). We say that \(x\) is a \(d_1\)-object if \(d(x) = d_1\). Finally, we assume that \(\{a_1, a_2, ..., a_p\} \subseteq A_{Fl}, \{b_1, b_2, ..., b_q\} \subseteq A_{St}\), \(a_{[i,j]}\) denotes a value of attribute \(a_i\), and \(b_{[i,j]}\) denotes a value of attribute \(b_i\) for any \(i, j\), and that

\[
 r = [a_{[1,1]} \land a_{[2,1]} \land ... \land a_{[p,1]}] \land [b_{[1,1]} \land b_{[2,1]} \land .... \land b_{[q,1]}] \rightarrow d_1
\]

is a classification rule extracted from \(S\) supporting some \(d_1\)-objects in \(S\). By \(sup(r)\) and \(conf(r)\), we mean the support and the confidence of \(r\), respectively. Class \(d_1\) is a preferable class and our goal is to reclassify \(d_2\)-objects into \(d_1\) class, where \(d_2 \in V_d\).
By an action rule schema \( r[d_2 \rightarrow d_1] \) associated with \( r \) and the reclassification task \( (d, d_2 \rightarrow d_1) \) we mean the following expression:

\[
\begin{align*}
  r[d_2 \rightarrow d_1] &= [(a_{1,1} \land a_{2,1} \land ... \land a_{p,1}) \land [(b_1, \rightarrow b_{1,1}) \land (b_2, \rightarrow b_{2,1}) \\
  &\land .... \land (b_q, \rightarrow b_{q,1})] \Rightarrow (d, d_2 \rightarrow d_1)].
\end{align*}
\]

In a similar way, by an action rule schema \( r[\rightarrow d_1] \) associated with \( r \) and the reclassification task \( (d, \rightarrow d_1) \) we mean the following expression:

\[
\begin{align*}
  r[\rightarrow d_1] &= [(a_{1,1} \land a_{2,1} \land ... \land a_{p,1}) \land [(b_1, \rightarrow b_{1,1}) \land (b_2, \rightarrow b_{2,1}) \\
  &\land .... \land (b_q, \rightarrow b_{q,1})] \Rightarrow (d, \rightarrow d_1)].
\end{align*}
\]

The term \([a_{1,1} \land a_{2,1} \land ... \land a_{p,1}]\) built from values of stable attributes, is called the header of the action rule \( r[d_2 \rightarrow d_1] \) and its values can not be changed.

The next step is to partition the supporting set of the action rule schemas into classes, each one generating corresponding action rule.

We adopt this strategy as the first step in our proposed method, and as an approach which allows for mining action rules from scratch [1, 5, 12], i.e. directly from the database without using pairs of classification rules. We therefore use an exhaustive method that would supply us with all important rules as a start.

3.2. Clustering

We are constructing the actions rules, by ”grabbing” supporting objects into action rules schema, directly from the database. The next step is to cluster action rules into groups, i.e. groups of rules, which are similar. Such grouping would allow us to combine the similar rules together later in the process.

We use a grid-based method, STING: STatistical INformation Grid [14]. We choose this method because of its advantage of fast processing time and its typical independence of the number of objects (scales well).

The spatial area is divided into rectangular cells. There are usually several levels of such cells, which form a hierarchical structure. Each cell at high level is partitioned into a number of smaller cells in the next lower level. Statistical information of each cell is calculated and stored beforehand. When finish examining the current layer, proceed to the next lower level. Repeat this process until the bottom layer is reached.

Let \( R = \{r_1, r_2, ..., r_k\} \) be the set of all action rules discovered by ARAS [5], and \( X = \bigcup_{i=1}^{k} \text{sup}(r_i) \), where \( \text{sup}(r_i) \) denotes the support of rule \( r_i \).

Running STING clustering on \( X \) produces \( \{X_1, X_2, X_3, ..., X_n\} \) as its partition representing the bottom layer \( R_i \) is defined as a set of action rules which are supported by objects in \( X_i \). It means that:
\[ R_i = \{ r \in R : X_i \cap \text{sup}(r) \neq \emptyset \} \]

for \( i = 1, 2, ..., n \).

By covering of \( R \) we mean \( \{ R_i : 1 \leq i \leq n \} \).

### 3.3. Generalization

Generalization of the data involves replacing low-level or "primitive" (raw) data with higher-level concepts through the use of concept hierarchies. For example, categorical attributes, like *street*, can be generalized to higher-level concepts, like *city* or *country*. Similarly, values of numerical attributes, like *age*, may be mapped to higher-level concepts, like *young*, *middle-aged*, and *senior*.

In this way, we form compact descriptions of raw data at different concept levels, which are called *summaries*. For that purpose, in this work we assume that attributes are hierarchical.

Since we have clustered the action rule space, we have ended up with \( n \) clusters, where each cluster contains a set \( R_n \) of similar rules. Next, we will generalize the attributes of these rules to create a summary, or a higher-level action rule. Each such summary will cover a certain portion of the action rule space; and, it may go outside its cluster boundary or overlap with another summary.

We will perform a generalization on every attribute. Thus, if we have two action rules \( r_1 \) and \( r_2 \) and the attribute value is not equal, then we go up in the hierarchy. If we have to go up to the highest/top level, then we drop the attribute. For example:

\[
\begin{align*}
r_1 &= \left( \left[ a_{1\!1\!2} \land b_{1\!2\!3} \land c_{1\!3\!4} \right] \land \left[ (e, e_{1\!2\!1} \rightarrow e_{1\!2\!3}) \land (f, f_{1\!2\!1} \rightarrow f_{1\!3}) \right] \right) \Rightarrow (d, d_1 \rightarrow d_2) \\
r_2 &= \left( \left[ b_{1\!3\!3} \land c_{1\!3\!5} \right] \land \left[ (e, e_{1\!3\!2} \rightarrow e_{1\!2\!4}) \right] \right) \Rightarrow (d, d_1 \rightarrow d_2) \\
G(r_1, r_2) &= \left( \left[ b_1 \land c_{1\!3\! } \right] \land \left[ (e, e_1 \rightarrow e_{1\!2\! }) \right] \right) \Rightarrow (d, d_1 \rightarrow d_2)
\end{align*}
\]

where \( G(r_1, r_2) \) is the generalization, or the summary, of \( r_1 \) and \( r_2 \).

### 4. Diversity of Summaries

A pattern, or a set of patterns, is diverse if its elements (or patterns in the set) differ significantly from each other. Diversity has been used as factor for measuring the interestingness of summaries.

Statistically, a summary can be considered diverse if its probability distribution is far from the uniform distribution. The more diverse a summary, the more interesting it is, because a user would commonly assume the uniform distribution. We are unaware of any existing research on using diversity to measure the interestingness of classification rules, or association rules [2].

Tzacheva [15] was the first to use diversity for action rules. The notion of diversity of action rule summaries was introduced by Tzacheva [15] as follows:
If we have two higher-level action rules \( r_1 \) and \( r_2 \), which have a big overlap in terms of the conditional part, then we say that the diversity \( \Delta \) of \( r_1 \) with respect to \( r_2 \) is low. Analogically, if the two action rules have a small overlap in their domains, then we say that the diversity \( \Delta \) of \( r_1 \) with respect to \( r_2 \) is high.

The diversity \( \Delta(r_1, r_2) \) is defined as: the number of different atomic terms including their positions, between the two rules. For example:

\[
\begin{align*}
  r_1 &= [a_2 \land b_1] \land [(c, c_1 \rightarrow e_2) \land (e, e_1 \rightarrow e_2)] \Rightarrow (d, d_1 \rightarrow d_2) \\
  r_2 &= [a_1 \land e_1] \land [(c, c_1 \rightarrow c_2) \land (f, f_1 \rightarrow f_2)] \Rightarrow (d, d_1 \rightarrow d_2) \\
  \Delta(r_1, r_2) &= 3 + 0 + 2 = 5
\end{align*}
\]

The same concept of action rule diversity can be applied to low-level action rules (non-generalized). In that sense, if two action rules have a big overlap (or low diversity), then they may be combined together to produce a generalized, or high-level action rule.

When the overlap is large, we are more safe to perform the generalization (combining of two rules). However, we would prefer a risky small overlap, because of diversity. Since the diversity is higher with small overlap, then the generalization we create will be more interesting.

Some overlaps will be ruled out as ‘bad’, since with the generalization it is possible that objects may shift into a class different from the original. Consider the following example (for clarity the action part is omitted):

\[
\begin{align*}
  r_3 &= [b_1 \land e_2] \Rightarrow d_1 \\
  r_4 &= [a_1 \land c_2] \land [(b_1 \land e_2)] \Rightarrow d_1 \\
  G(r_3, r_4) &= [(b \land e_2)] \Rightarrow d_1
\end{align*}
\]

At the same time we have another rule \( r_5 \) which implies a different class - \( d_2 \):

\[
\begin{align*}
  r_5 &= [(b_2 \land e_2)] \Rightarrow d_2
\end{align*}
\]

If we generalize \( b_1 \) and \( b_2 \) into \( b \), as shown in \( G(r_3, r_4) \), then \( b \) also covers \( b_2 \) from the rule \( r_5 \), which however has a different decision part, i.e. implies \( d_2 \). It means that if we perform the generalization \( G(r_3, r_4) \), some objects will shift into a class different from the intended one. Therefore, we cannot combine the \( r_3 \) and \( r_4 \) rules together.

5. Cost and the Hierarchy

Typically, there is a cost associated with changing an attribute value from one class to another - more desirable one. The cost is a subjective measure, in a sense that domain knowledge from the user or experts in the field is necessary in order to determine the costs associated with taking the actions. Costs could be monetary, moral, or a combination of the two. For example, lowering the interest percent rate for a customer is a monetary cost for the bank; while, changing the marital status from ‘married’ to ‘divorced’ has a moral cost, in addition to any
monetary costs which may be incurred in the process. Feasibility is an objective
measure, i.e. domain independent.

According to the cost of actions associated with the classification part of
action rules, a business user may be unable or unwilling to proceed with them.

The definition of cost was introduced by Tzacheva and Ras [6] as follows:
Assume that $S = (X, A, V)$ is an information system. Let $Y \subseteq X$, $b \in A$ is
a flexible attribute in $S$ and $v_1, v_2 \in V_b$ are its two values. By $\mathcal{P}_S(b, v_1 \rightarrow v_2)$
we mean a number from $(0, \omega]$ which describes the average cost of changing the
attribute value $v_1$ to $v_2$ for any of the qualifying objects in $Y$. These numbers
are provided by experts. Object $x \in Y$ qualifies for the change from $v_1$ to $v_2$, if
$b(x) = v_1$. If the above change is not feasible, then we write $\mathcal{P}_S(b, v_1 \rightarrow v_2) = \omega$.
Also, if $\mathcal{P}_S(b, v_1 \rightarrow v_2) < \mathcal{P}_S(b, v_3 \rightarrow v_4)$, then we say that the change of values
from $v_1$ to $v_2$ is more feasible than the change from $v_3$ to $v_4$. Assume an action
rule $r$ of the form:

$$(b_1, v_1 \rightarrow w_1) \land (b_2, v_2 \rightarrow w_2) \land \ldots \land (b_p, v_p \rightarrow w_p) \Rightarrow (d, k_1 \rightarrow k_2)$$

If the sum of the costs of the terms on the left hand side of the action rule
is smaller than the cost on the right hand side, then we say that the rule $r$ is feasible.

Once we have created the higher-level action rules, or the action rule sum-
maries, we may examine the cost associated with each summary. Clearly, the
summaries of low cost are more actionable, i.e. easier for the user to accomplish.
Therefore, they are more interesting.

Hence, if the summary has high cost, we may disregard it as being of low
interest to the user. In this way, we would further decrease the space of the
mined action rules. In addition, it is possible that if the summary is not inter-
esting, then we may make assumptions about the interestingness of the whole
cluster, from which the summary was extracted. However, in order to make
such determinations, the correlations of the attributes will need to be taken into consideration. Little, to no work has been done examining the correlations of attributes with action rule discovery.

The work in Tzacheva [15] suggested removing the high cost rules, when creating summaries, in order to additionally decrease the space of action rules. In this work, we propose computing the cost of the summaries by taking an average of the costs of the composing terms. In this way, cost decreases as we go up in the hierarchy, because some terms are removed with the generalization.

6. Algorithm for generalization of action rules to create summaries

The algorithm discovers summaries by maximizing the diversity and minimizing the cost. The summaries fall within the user defined confidence threshold.
Algorithm:

\[ \Delta(R_i) := \{ \Delta(r_1, r_2) : r_1, r_2 \in R_i \} \]

for every \( i, j \) \( \text{mark}(r_i, r_j) := 0 \)

\[ \{ \]

\( (r_i, r_j) := (r_1, r_2) \) where \( \Delta(r_1, r_2) = \text{MAX} (\Delta(R_i)) \)

if \( \text{conf}(G(r_i, r_j)) \geq \lambda \)

\( R_i := R_i \cup \{ G(r_i, r_j) \} \)

\( \text{mark}(r_i, r_j) := 1 \)

\} while \( \text{mark}(r_i, r_j) = 0 \)

for every \( r_i \)

if \( [r_i, G(r_i, r_j) \notin R_i] \)

\( R_i := R_i - r_i \)

7. Conclusions and Future Work

In this work, we present an improved method to decrease the space of action rules, through the creation of summaries, and the use of hierarchical attributes. The new algorithm produces summaries by maximizing the diversity of rule pairs, and minimizing the cost of the suggested actions. We, therefore, provide means for reducing the volume of the mined results, and supply the user with short general descriptions of high interest actionable knowledge.

Diversity is a major criterion for measuring summaries, but no work has been done so far to study the diversity of either association, or classification \([2]\) rules. Tzacheva \([15]\) was the first to use the notion of diveristy with action rules summaries. The notion is used within the generalization process in a sense that if two low-level action rules have a big overlap (low diversity), then they may be combined together to produce a high-level rule, or a summary. In addition, the more diverse a set of low-level action rules is, the more interesting it is, since it will convey more knowledge to the user compared to a set with too many similar rules.

With the proposed algorithm in this work, we extend diversity of action rule summaries by choosing to merge the pair of two rules, which has the maximum diversity.

We consider the cost of action rule summaries, as well. The summaries of low cost are more actionable, i.e. easier for the user to accomplish, and therefore more interesting. Tzacheva \([15]\) disregarded the ones with high cost as being of
low interest to the user. In this work, we suggest an average approach to computing the cost, which leads to cost decrease as we go up in the generalization hierarchy.

Directions for the future include employing a more generic approach for creating summaries, which would allow for using non-hierarchical attributes as well. For instance, taking intervals with numerical values, or a subset for non-numerical ones. Clearly, the effect on the precision and recall of summaries needs to be taken into consideration in such case.

The scalability issue with the number of action rules produced, may be dealt with by introducing user-defined thresholds on support and confidence. Semantic connections of the rules with the diversity measured require further studies; as well as, the computational complexity of the algorithm. Experiments with application domain data need to be performed to supplement this theoretical method.

Other future work could integrate the summarization of action rules into some of the approaches in the previous work - section 2, as means for decreasing the action rule space of the mined results.

In addition, with action rules, further work is needed in order to study the degree with which a suggested action succeeds in changing the class to a more desirable one; or, the prediction of unexpected effects/causes, which may occur after the action has been performed.

Applicable fields are: business, financial, medical, industrial.

References:
Set Symposium (JRS07) Conference on Rough Sets, Fuzzy Sets, Data Mining and Granular Computing.


