

Discovery of concept expansions

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Abstract. Robot-discoverers and other intelligent systems should interact with the physical world in complex, yet purposeful and accurate ways. Knowledge representation which is internal to a computer lacks empirical meaning and thus it is insufficient for the investigation of the external world. We argue that operational definitions are necessary to provide empirical meaning of concepts, but they have been largely ignored by the research on automation of discovery. In this paper we reconstruct the scientific mechanism by which operational definitions are created and we make several steps towards the implementation. Individual operational definitions can be viewed as algorithms that operate in the real world. They can and they should be improved in the course of interaction with the real world, so that their accuracy is improved. We explain why many operational definitions are needed for each concept and how different operational definitions of the same concept can be empirically and theoretically equivalent. We argue that all operational definitions of the same concept must form a coherent set and we define the meaning of coherence. No set of operational definitions is complete. We argue that expanding the operational definitions is one of the key tasks in science. Among many possible expansions only a very special few lead to a satisfactory growth of scientific knowledge. While our examples come from natural sciences, where the use of operational definitions is especially clear, operational definitions are needed for all empirical concepts. We briefly argue their role in a robot-discoverer and in database applications.

1 Operational definitions provide empirical meaning

Data about external world are obtained by observation and experiment. Sophisticated procedures and instruments are commonly used to reach data of scientific value. Yet we rarely think systematically about methods by which data have been procured, until problems occur. When a set of data is inconsistent with our expectations, we start asking: “How was this particular measurement obtained?”, “What method has been used?”, “How is this method justified?”. Often it turns out that a method must be changed. Because data can be wrong in so many ways, considerable knowledge is required in order to examine and improve measurement methods.

It is critical to the growth of scientific knowledge to study new situations, for which no known method can measure a particular quantity. For instance,

we may wish to measure temperatures lower than the capabilities of all existing instruments. Or we want to measure temperature change inside a living cell, as the cell undergoes a specific process.

When no known method applies, new methods must be discovered. We use the term “discovery” rather than “invention” since measurement methods can be verified, as we will demonstrate later. New measurement methods must expand the existing concepts. For instance, a new thermometer must produce measurements on a publicly shared scale of temperature.

Discovery of new methods, which we also call operational definitions, is the central problem in this paper. We present a systematic solution to the quest for new operational definitions. We provide an algorithm that demonstrates how empirical knowledge is used to construct new operational definitions, how new methods can be empirically verified and how choices can be made among competing methods.

At the end of each section we make a few basic claims about operational definitions.

Claim 1: For each empirical concept, measurements must be obtained by methods which are repeatable, can be explained in detail and can be used in different laboratories.

Claim 2: The actual verification in empirical science is limited to what can be empirically examined. The scope of operational definitions determines the scope of scientific verification.

Claim 3: In contrast, scientific theories often make claims beyond the facts that can be empirically verified at a given time. Theoretical claims often apply to all physical situations, whether we can observe them or not.

In this paper we restrict our attention to numerical properties of objects and their pairs. The numbers that result from measurements, for instance temperature or distance, we call *values* of empirical concepts.

Claim 4: In additions to methods that return values of properties, all types of empirical concepts require operational definitions, for instance relations between empirical objects and special situations, that may be recognized or created, such as the triple point of water.

Claim 5: Some operational definitions provide data; other definitions prepare objects that possess specific properties.

Claim 6: Operational definitions apply to objects, states, events, locations and other empirical entities.

2 The AI research has neglected operational definitions

Operational semantics links the terms used in scientific theories with direct observations and manipulations (Bridgman, 1927; Carnap, 1936). While important in empirical science, the mechanisms that produce high quality experiments have been neglected not only in the existing discovery systems but in the entire domain of artificial intelligence.

The distinction between formalism and its interpretation, also called semantics, has been applied to the study of science since 1920's and 1930's. Scientific theories have been analyzed as formal systems whose language is empirically interpreted by operational definitions.

A similar distinction applies to discovery systems and to knowledge they create. A discovery mechanism such as BACON (Langley, Simon, Bradshaw & Zytkow, 1987) can be treated as (1) a formal system that builds equations from data that are treated formally as tuples in the empirical space of the values of independent and dependent variables plus (2) a mechanism that procures data.

Similarly to scientists, BACON and other discovery systems use plans to propose sequences of experiments. Each experiment consists in preparing an empirical situation, described by a list of values x_1, \dots, x_k of empirical variables X_1, \dots, X_k , and by measuring the value y of a dependent variable Y which provides the "world response" to the empirical situation characterized by x_1, \dots, x_k .

Instead of real experiments, BACON procures data by two mechanisms. In one mechanism the list of values of independent variables becomes the argument to a PRINT statement, followed by READ, to which a user must type the appropriate value of the dependent variable. The other mechanism generates data by simulation. The values of independent variables are passed on as arguments to a function call that computes the value of the dependent variable.

This treatment bypasses real experimentation and measurements. In the wake of robotic discovery systems, operational semantics must, at the minimum, provide realistic methods to acquire data. Even papers and collections that consider many components of the scientific methods (Kulkarni & Simon, 1987; Sleeman, Stacey, Edwards & Gray, 1989; Shrager & Langley, 1990; Valdes-Perez, 1995) neglect operational definitions of concepts.

Little has been done thus far to remedy this deficiency. Żytkow, Zhu & Hussam (1990) used a robotic mechanisms which conducted automatically experiments under the control of FAHRENHEIT. In another robotic experiment, Żytkow, Zhu & Zembowicz (1992) used a discovery process to refine an operational definition of mass transfer. Huang & Zytkow (1997) developed a robotic system that repeats Galileo's experiment with objects rolling down an inclined plane. One operational definition drove the robot arm so that it deposited a cylinder on the top of an inclined plane, while another measured the time in which the cylinder rolled to the bottom of the plane.

While operational semantics must accompany any formalism that applies to the real world, it has been neglected in AI. Jackson's claim (1990) is typical: "a well-defined semantics ... reveals the meaning of ... expressions by virtue of their form." But this simply passes on the same problem to a broader formalism, that includes all the terms used in formal semantics. Those terms also require real-world interpretation that must be provided by operational definitions.

Plenty of further research must be conducted to capture the mechanisms in which operational definitions are used in science and to make them applicable on intelligent robots.

Claim 7: Formal semantics are insufficient to provide empirical meaning.

Claim 8: Robotic discoverers require operational definitions.

3 Operational definitions interact with the real world

Early analyses of operational definitions used the language of logic. For instance, a dispositional property “soluble in water” has been defined as

If x is in water then (x is soluble in water if and only if x dissolves)

But a more adequate account is operational rather than descriptive:

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Soluble (x)
  Put x in water!
  Does x dissolve?
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An operational definition, treated as an algorithm, consists of instructions that prescribe manipulations, measurements and computations on the results of measurements. Iteration can enforce the requirements such as temperature stability, which can be preconditions for measurements. Iteration can be also used in making measurements. The loop exit condition such as the equilibrium of the balance, or a coincidence of a measuring rod with a given object, marks the completion of a step in the measurement process.

Two types of procedures differentiate between independent and dependent variables. They can be contrasted as manipulation and measurement mechanisms. Each independent variable can be set by a manipulation mechanism to a specific value, while a response value of an dependent variable is obtained by a measurement mechanism. In this paper we focus on measurement procedures.

It may happen that a particular instruction within procedure P would not work in a specific situation. A thermal equilibrium cannot be reached or thermometric liquid freezes. In those cases P cannot be used. Each procedure may fail for many reasons. Some of these reasons may be systematic. For instance, a given thermometer cannot measure temperatures below -40°C and above 100°C ; it can only measure temperature of objects in direct thermal contact. Let us call the range of procedure P by R_P .

Often, a property is measured indirectly. Consider distance measurement by sonar or laser. The time interval is measured between the emitted and the returned signal. Then the distance is calculated as a product of time and velocity. Let $C(x)$ be the quantity measured by procedure P . When P terminates, the returned value of C is $f(m_1, \dots, m_k)$, where m_1, \dots, m_k are the values of different quantities measured or generated by instructions within P , and f is a computable function on those values.

Claim 9: Each operational definition can be treated as an algorithm.

Claim 10: The range of each procedure is limited in many ways, thus each operational definition P is a partial definition applicable in the range R_P .

Claim 11: An operational definition of concept C can measure different quantities and use empirical laws to determine the value of C : $C(x) = f(m_1, \dots, m_k)$

Claim 12: An operational definition for a concept $C(x)$ can be represented by a descriptive statement: “If x is in R_P then $C(x) = f(m_1, \dots, m_k)$ ”

4 Each concept requires many operational definitions

In everyday situations distance can be measured by a yard-stick or a tape. But a triangulation method may be needed for objects divided by a river. Measuring rod cannot be used to find the distance from the Earth to the Sun and the Moon, while the triangulation method will work in both cases. Then, after we have measured the diameter of the Earth orbit around the Sun, we can use triangulation to measure distances to many stars.

But there are stars for which the difference between the “winter” angle and the “summer angle” measured on the Earth, is non-measurably small, so another method of distance measurement is needed. Some of the stars within the range of triangulation are called cefeids. They pulsate and it has been determined that their maximum brightness varies according to the logarithm of periodicity. Another law, determined on Earth and applied to stars claims that the perceived brightness of a given constant light source diminishes with distance as $1/d^2$. This law jointly with the law for cefeids allows us to determine the distance to galaxies in which individual cefeids are visible.

For such galaxies the Hubble Law has been empirically discovered. It claims proportionality between the distance and red shift in the lines of hydrogen spectrum. The law of red shift has been used to determine the distance of the galaxies so distant that cefeids cannot be distinguished.

Similarly, while a gas thermometer applies to a large range of states, in very low temperatures any gas freezes or gas pressure becomes non-measurably small. A thermometer applied in those situations measures magnetic susceptibility of paramagnetic salts and uses Curie-Weiss Law to compute temperature. There are states of high temperature in which no vessel can hold a gas, and other states in which the inertia of gas thermometer has unacceptable influence on the measured temperature. Measurements of thermal radiation and other methods can be used in many such cases.

Claim 13: Empirical meaning of a concept is defined by a set of operational definitions.

Claim 14: Each concrete set is limited and new methods must be constructed for objects beyond those limits.

5 Methods can be empirically and theoretically equivalent

Consider two operational definitions P_1 and P_2 that measure the same quantity C . When they apply to the same objects their results should be empirically equivalent within the accuracy of measurement. If P_1 and P_2 provide different results, one or both must be adjusted until the empirical equivalence is regained.

From the antiquity it has been known that triangulation provides the same results, within the limits of measurement error, as a direct use of measuring rod or tape. But in addition to the empirical study of equivalence, procedures can

be compared with the use of empirical theories and their results may be proven to be equal.

Triangulation uses a basic theorem of Euclidean geometry: one side and two adjacent angles in a triangle uniquely determine the remaining sides. This justifies theoretically the consistency of two methods: by the use of yard-stick and by triangulation. Since, or to the extent in which, Euclidean geometry is valid in the physical world, whenever we make two measurements of the same distance, one using a rod or a tape while the other using triangulation, the results are consistent.

A value returned by a procedure may not be physically adequate. The measurement can affect the measured quantity. This principle has been justified in quantum mechanics, but it must be considered even in the range of classical measurements. When a thermometer reaches thermal equilibrium with the measured body b , the temperature of b can be changed drastically. The thermal inertia of a thermometer should be adequate to the task.

Claim 15: Methods can differ by their accuracy and by degree to which they influence the measured quantity.

Claim 16: Inadequacy of the measured results limits the range of operational definitions.

Claim 17: When two operational definitions define the same property and apply to the same objects, their results should be empirically equivalent.

Claim 18: When two operational definitions define the same concept $C(x)$, it is possible to prove their equivalence. The prove consists in deducing from a verified empirical theory that the statements that represent them are equivalent, that is, $f_1(m_1, \dots, m_k) = f_2(n_1, \dots, n_l)$

Claim 19: When the statements that represent two procedures use empirical laws $C(x) = f_1(m_1, \dots, m_k)$, $C(x) = f_2(n_1, \dots, n_l)$, theoretical equivalence of both procedures follows from those laws.

Claim 20: The more general and better verified are the theories that justify the equivalence of two procedures P_1 and P_2 , the stronger are our reasons to believe in the equivalence of P_1 and P_2 .

Claim 21: Proving the equivalence of two procedures is desired, because often the empirical verification of equivalence is costly or practically impossible.

6 Operational definitions of a concept form a coherent set

We have considered several procedures that measure distance. But distance can be measured in many other ways. Even the same method, when applied in different laboratories, varies in details. How can we determine that different measurements define the same physical concept? The meaning can be coordinated by the requirements of empirical and theoretical equivalence in the areas of common application. However, we must also require that each method overlaps with some other methods and further, that each two methods are connected by a chain of overlapping methods.

Definition: A set $\Phi = \{\phi_1, \dots, \phi_n\}$ of operational definitions is coherent **iff** for each $i, j=1, \dots, n$:

(1) ϕ_i is empirically equivalent with ϕ_j . Notice that this condition is trivially satisfied when the ranges of both operational definitions do not overlap;

(2) there is a sequence of definitions $\phi_{-i_1}, \dots, \phi_{-i_k}$, such that $\phi_{-i_1} = \phi_i$, $\phi_{-i_k} = \phi_j$, and for each $m = 2, \dots, k$ the ranges of ϕ_{-i_m} and $\phi_{-i_{m+1}}$ intersect.

The measurements of distance in our examples form such a coherent set. Rod measurements overlap with measurements by triangulation. Different versions of triangulation overlap with one another. The triangulation applied to stars overlaps with the method that uses cefeids, which in turn overlaps with the method that uses red shift and Hubble Law.

Similarly, the measurements with gas thermometer have been used to calibrate the alcohol and mercury thermometers in their areas of joint application. For high temperatures, measurements based on the Planck Law of black body radiation overlap with the measurements based on gas thermometers. For very low temperatures, the measurements based on magnetic susceptibility of paramagnetic salts overlap with, and are empirically equivalent to, measurements with the use of gas thermometer.

Claim 22: Each empirical concept should be defined by a coherent set of operational definitions. Historically there are cases when the coherence is missing, but the discovery of a missing link becomes a challenge.

For instance, the experiment of Millikan provided a link between the charge of electron and electric charges measured by macroscopic methods.

Claim 23: By examining a coherent set Φ of operational definitions we can demonstrate that the values measured by all procedure in Φ are on the same scale.

Claim 24: In the case of conflict between different methods, additional data are collected and methods are adjusted in order to restore the coherence.

Claim 25: Operational definitions provide means to expand to new areas the range of the laws they use.

7 Laws can be used to form new operational definitions

For each concept, operational definitions can be expanded in several obvious directions, to reach very small values, very large values, and values that are very precise. But the directions are far more numerous. Within the range of “room” temperatures, consider the temperature inside a cell, or temperature of a state that is fast varying and must be measured every second. Or consider the measurement of temperature on the surface of Mars. Each of these cases requires different methods. A scientist who wants to examine the shift of tectonic plates may do so by comparing the distances on the order of tens of kilometers over the time period of a year, if the accuracy of measurement is below a millimeter.

Whenever we consider expansion of the range of operational definitions for an empirical concept C , the situation is similar:

(1) we can observe objects in a new range R for which C cannot be measured with the sufficient accuracy;

(2) some other attributes A_1, \dots, A_n of objects in R can be measured, or else those objects would not be empirically available at all;

(3) some of the measured properties are linked to C by empirical laws or theories.

We can use one or more of those laws in a new method: measure some of A_1, \dots, A_n and then use laws to compute the value of C . For example,

The task:

determine distance D from Earth to each in a set R of galaxies,
given some of the measured properties of R : A_1, A_2, \dots, A_n ;
(this presupposed operational definitions for A_1, \dots, A_n in the range R)
For instance, let A_2 measure the redshift of hydrogen spectrum.
Let $D=h(A_2)$ be Hubble Law

The new method is:

For a galaxy g , when no individual cefeids can be distinguished:
Measure A_2 of the light coming from g by a method of spectral analysis
Compute the distance $D(\text{Earth}, g)$ as $h(A_2(g))$

Some laws that apply to galaxies cannot be used. Consider the law $D = a/\sqrt{\text{brightness}}$. It applies even to the most remote sources of light. But the brightness that is used in the law is the absolute brightness at the source, not the brightness perceived by an observer. Should we have a way of determining the absolute brightness, we could determine the distance to galaxies by the inversed square root law. When the distance to galaxies can be determined, however, we know from observations that galaxies at the same distance have different brightness.

A schema similar to the application of Hubble Law applies to other operational definitions that determine distance. Properties measurable in a new range can be yearly parallax, perceived brightness, shape, electromagnetic spectrum, and so on. The same algorithm can be used in many applications:

Algorithm:

Input: set of objects observed in range R
attribute C that cannot be measured in R
set of attributes A_1, \dots, A_k that can be measured in R
set $\{F_1, \dots, F_p\}$ of known operational definitions for C
set LAWS of known empirical laws
Output: a method by which the values of C can be determined in R

Seek in LAWS a law L in which C occurs

Let B_1, \dots, B_m be the remaining attributes that occur in L
Verify that C can be computed from L , and the values of B_1, \dots, B_m
Verify that $\{B_1, \dots, B_m\}$ is subset of $\{A_1, \dots, A_k\}$,
that is, B_1, \dots, B_m can be measured in at least some situations in R
Use L and B_1, \dots, B_m to create new procedure F for C
Make F consistent with procedures in $\{F_1, \dots, F_p\}$

After the first such procedure has been found, the search may continue:

For each law that involves C , try to build an operational definitions of C

In set-theoretic terms, each expansion of concept C to a new range R can be viewed as a mapping from the set of distinguishable classes of equivalence with respect to C for objects in R to a set of possible new values of C , for instance, the values larger than those that have been observed with the use of the previous methods. But possible expansions are unlimited. The use of an existing law narrows down the scope of possible concept expansions to the number of laws for which the above algorithm succeeds. But the use of an existing law does not merely reduce the choices, it also justifies them. Which of the many values that can be assigned to a given state corresponds to its temperature? If laws reveal the real properties of physical objects, then the new values which fit a law indicate concept expansion which has a potential for the right choice.

Claim 26: Whenever the empirical inquiry expands to new territories, new discoveries follow. New procedures are instrumental to that growth.

Claim 27: Each new procedure expands the law it uses to a new range.

If a number of procedures provide alternative concept expansions, various selection criteria can be used, depending on the goal of research. Operational definitions can differ by their range, accuracy, the degree to which they can be verified in the new area, and so on.

Claim 28: Among two methods, the one which has a broader range is preferred, for it justifies concept expansion by a broader expansion of an existing law.

Claim 29: Among two methods, one which has a higher accuracy is preferred, for it provides more accurate data and thus a stronger empirical foundation for the expansion of empirical theories.

Claim 30: Methods must be verified in their new area of application or else, the empirical laws they apply would be mere definitions.

Claim 31: If two procedures P_1 and P_2 use laws L_1 and L_2 respectively, and produce empirically inconsistent results for new objects in range R , the choice of P_1 will make L_2 false in R .

8 Operational definitions apply to all empirical concepts

While explicit operational definitions are rarely formed by human experimental scientists, they become necessary in autonomous robots. A robot explorer can also benefit from mechanisms for generation of new procedures. Realizing that a given operational procedure P cannot be applied in a given situation, the robot should be able to use its knowledge and replace P by an equivalent procedure P_1 . Using our computational mechanism, the robot can find out that P and P_1 are not only theoretically equivalent with regard to robot's knowledge, but are also empirically equivalent when both can be used.

Operational meaning should be extended to databases. They are repositories of facts that should be shared publicly or among allied institutions as a major resource for knowledge discovery and verification. But data and knowledge can be only useful for those who understand their meaning. Operational definitions describe how the values in a given field been produced.

Operational definitions can be generated from data and applied in different databases. Consider a regularity L , discovered in a data table D , which provides accurate predictions of attribute C from known values of A_1, \dots, A_n . L can be used as a method that determines values of C .

Consider now another table D_1 , that contains data that describe similar situations but uses slightly different attributes than D . Instead of test C , some other tests B_1, \dots, B_m are provided, which may or may not be compatible with C . Suppose that a doctor who has been familiar with test C at his previous workplace, issues a query against D_1 that includes attribute C which is not in D_1 . A regular query answering mechanism would fail, but a mechanism that can expand operational meaning of concepts may handle such a query (Ras, 1997). A quest Q for operational definition of concept C with the use of B_1, \dots, B_m will be send to other databases. If an operational definition is found, it is used to compute the values of C in the doctor's query.

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