

**Problem**

For the information system given below, find the set of rules describing C in terms of E, F, G by following ERID algorithm. Use 1/2 for minimum confidence and 1/2 for minimum support.

Assume that Dom(E)={e1,e2}, Dom(F)={f1, f2}, Dom(C)={c1,c2}, G={g1,g2}.

Use Chase with threshold 1/3 to check if C(x3) will change its value based on discovered rules.

X	E	F	G	C
x1	e1	f1	(g1,1/2)(g2,1/2)	c2
x2	e2	f1	g2	c1
x3	(e1,1/2)(e2,1/2)	f1	g1	(c1,1/2)(c2,1/2)
x4	e2	(f1,1/2)(f2,1/2)	g2	c1
x5	e1	f2	g1	c2
x6	e2	f2	(g1,1/2)(g2,1/2)	c1

$$e1^* = \{(x1,1), (x3,1/2), (x5,1)\}, e2^* = \{(x2,1), (x3,1/2), (x4,1), (x6,1)\}$$

$$f1^* = \{(x1,1), (x2,1), (x3,1), (x4,1/2)\}, f2^* = \{(x4,1/2), (x5,1), (x6,1)\}$$

$$g1^* = \{(x1,1/2), (x3,1), (x5,1), (x6,1/2)\}, g2^* = \{(x1,1/2), (x2,1), (x4,1), (x6,1/2)\}$$

$$c1^* = \{(x2,1), (x3,1/2), (x4,1), (x6,1)\}, c2^* = \{(x1,1), (x3,1/2), (x5,1)\}$$

$$e1 \rightarrow c1 \text{ sup} = 1/2 * 1/2 = 1/4 \quad e1 \rightarrow c2 \text{ sup} = 1 * 1 + 1/2 + 1 * 1 = 9/4, \text{ conf} = 9/4 : 5/2 = 18/20$$

$$e2 \rightarrow c1 \text{ sup} = 1 * 1 + 1/2 * 1/2 + 1 * 1 + 1 * 1 = 13/4 \quad \text{conf} = 13/12 : 7/2 = 26/84 \quad e2 \rightarrow c2 \text{ sup} = 1/4$$

$$f1^* = \{(x1,1), (x2,1), (x3,1), (x4,1/2)\} \quad f2^* = \{(x4,1/2), (x5,1), (x6,1)\}$$

$$f1 \rightarrow c1 \text{ sup} = 1 * 1 + 1 * 1/2 + 1 * 1/2 = 2 \quad \text{conf} = 2 : 7/2 \quad f1 \rightarrow c2 \text{ sup} = 1 * 1 + 1 * 1/2 = 3/2, \text{ conf} = 3/2 : 7/2 = 6/14$$

$$f2 \rightarrow c1 \text{ sup} = 1 * 1/2 + 1 * 1 = 3/2 \quad \text{conf} = 3/2 : 5/2 = 6/10 \quad f2 \rightarrow c2 \text{ sup} = 1 * 1 = 1, \text{ conf} = 1 : 5/2 > 1/2$$

$$g1^* = \{(x1,1/2), (x3,1), (x5,1), (x6,1/2)\} \quad g2^* = \{(x1,1/2), (x2,1), (x4,1), (x6,1)\}$$

$$g1 \rightarrow c1 \text{ sup} = 1 * 1/2 + 1/2 * 1 = 1, \text{ conf} = 1 : 3 \quad g1 \rightarrow c2 \text{ sup} = 1/2 * 1 + 1 * 1/2 + 1 * 1 = 2, \text{ conf} = 2 : 3$$

$$g2 \rightarrow c1 \text{ sup} = 1 * 1 + 1 * 1 + 1 * 1 = 3, \text{ conf} = 3 : 7/2 \quad g2 \rightarrow c2 \text{ sup} = 1 * 1/2, \text{ conf} = 1/2 : 7/2$$

$$f1 * g2 \rightarrow c2 \text{ sup} = 1 * 1/2, \text{ conf} = 1/2 : 2 \quad f2 * g2 \rightarrow c2 \text{ sup} = 0$$

$$f1.g2^* = \{(x1,1/2), (x2,1), (x4,1/2)\} \quad f2.g2^* = \{(x4,1/2), (x6,1/2)\}$$

$$c(x3): \quad c2 - 1/2 * 9/4 * 18/20 + 1 * 2 * 2/3 = n1$$

$$c1 - 1/2 * 13/4 * 13/42 + 1 * 2 * 4/7 = n2$$

$$c(x3) = \{(c2, n1/(n1+n2)), (c1, n2/(n1+n2))\}$$