Throughout we use both the notations $\binom{n}{r}$ and C_r^n for the number $\frac{n!}{(n-r)!r!}$.

1. How many paths consisting of a sequence of horizontal and/or vertical line segments with each segment connecting a pair of adjacent letters in the diagram below, is the word **CONTEST** spelled out as the path is traversed from beginning to end?

- Recall that a Yahtzee Roll is a roll of five indistinguishable dice.
 a. How many different Yahtzee Rolls are possible?
 b. How many Yahtzee Rolls have exactly 3 different numbers showing?
- 3. How many numbers can be expressed as a sum of three distinct members of the set {4, 5, 6, 7, 8, 9, 10, 11, 12}?
- 4. Let $S = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}.$
 - a. How many five element subsets does the set have?
 - b. How many subsets of S have an odd number of members?
 - c. How many subsets of S have 1 as a member?
 - d. How many subsets have 1 as a member and do not have 2 as a member?
- 5. Imagine that the 4×7 grid of squares below represents the streets of a part of the city where you live. You must walk 11 blocks to get from the lower left corner at A to the upper right corner at B.
 - (a) How many different 11 block walks are there?
 - (b) How many 11 block walks avoid the terrible corner marked with the bullet?
 - (c) How many 11 block walks go through the terrible corner?
 - (d) How many different 12 block walks are there from A to B?
 - (e) How many different 13 block walks are there from A to B?



- 6. How many four-digit numbers have the property that the sum of the first three digits is the fourth digit. For example 1247 has the property.
- 7. How many numbers in the set {100, 101, 102, ..., 999} have a sum of digits equal to 9? B. How many four digit numbers have a sum of digits 9? C. How many integers less than one million have a sum of digits equal to 9? November 14, 2005 2:37 P.M.