1. If a and b are digits for which

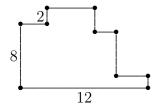
then a + b =

- **(A)** 3
- **(B)** 4
- (C) 7
- **(D)** 9
- **(E)** 12

2. The adjacent sides of the decagon shown meet at right angles. What is its perimeter?



- **(B)** 32
- (C) 34
- **(D)** 44
- **(E)** 50



3. If x, y, and z are real numbers such that

$$(x-3)^2 + (y-4)^2 + (z-5)^2 = 0,$$

then x + y + z =

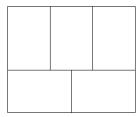
- **(A)** -12
- **(B)** 0
- **(C)** 8
- **(D)** 12
- **(E)** 50

4. If a is 50% larger than c, and b is 25% larger than c, then a is what percent larger than b?

- (A) 20%
- **(B)** 25%
- **(C)** 50%
- **(D)** 100%
- **(E)** 200%

5. A rectangle with perimeter 176 is divided into five congruent rectangles as shown in the diagram. What is the perimeter of one of the five congruent rectangles?

- **(A)** 35.2
- **(B)** 76
- **(C)** 80
- **(D)** 84
- **(E)** 86



6. Consider the sequence

$$1, -2, 3, -4, 5, -6, \ldots,$$

whose n^{th} term is $(-1)^{n+1} \cdot n$. What is the average of the first 200 terms of the sequence?

- **(A)** -1
- **(B)** -0.5
- **(C)** 0
- **(D)** 0.5
- (E) 1

7. The sum of seven integers is -1. What is the maximum number of the seven integers that can be larger than 13?

- **(A)** 1
- **(B)** 4
- (C) 5
- **(D)** 6
- (\mathbf{E}) 7

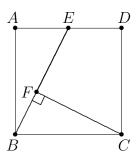
8. Mientka Publishing Company prices its best seller Where's Walter? as follows:

$$C(n) = \begin{cases} 12n, & \text{if } 1 \le n \le 24, \\ 11n, & \text{if } 25 \le n \le 48, \\ 10n, & \text{if } 49 \le n, \end{cases}$$

where n is the number of books ordered, and C(n) is the cost in dollars of n books. Notice that 25 books cost less than 24 books. For how many values of n is it cheaper to buy more than n books than to buy exactly n books?



9. In the figure, ABCD is a 2×2 square, E is the midpoint of \overline{AD} , and F is on \overline{BE} . If \overline{CF} is perpendicular to \overline{BE} , then the area of quadrilateral CDEF is



(A) 2 (B)
$$3 - \frac{\sqrt{3}}{2}$$
 (C) $\frac{11}{5}$ (D) $\sqrt{5}$

(C)
$$\frac{11}{5}$$

(D)
$$\sqrt{5}$$

(E)
$$\frac{9}{4}$$

10. Two six-sided dice are fair in the sense that each face is equally likely to turn up. However, one of the dice has the 4 replaced by 3 and the other die has the 3 replaced by 4. When these dice are rolled, what is the probability that the sum is an odd number?

(A)
$$\frac{1}{2}$$

(B)
$$\frac{4}{9}$$

(C)
$$\frac{1}{2}$$

(D)
$$\frac{5}{9}$$

(A)
$$\frac{1}{3}$$
 (B) $\frac{4}{9}$ (C) $\frac{1}{2}$ (D) $\frac{5}{9}$ (E) $\frac{11}{18}$

11. In the sixth, seventh, eighth, and ninth basketball games of the season, a player scored 23, 14, 11, and 20 points, respectively. Her points-per-game average was higher after nine games than it was after the first five games. If her average after ten games was greater than 18, what is the least number of points she could have scored in the tenth game?

- (A) 26
- **(B)** 27
- (C) 28
- **(D)** 29
- **(E)** 30

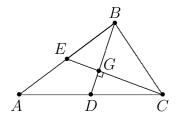
12. If m and b are real numbers and mb > 0, then the line whose equation is y = mx + b cannot contain the point

- (A) (0, 1997) (B) (0, -1997) (C) (19, 97) (D) (19, -97) (E) (1997, 0)

13. How many two-digit positive integers N have the property that the sum of N and the number obtained by reversing the order of the digits of N is a perfect square?

- **(A)** 4
- **(B)** 5
- **(C)** 6
- **(D)** 7
- **(E)** 8

- 14. The number of geese in a flock increases so that the difference between the populations in year n+2 and year n is directly proportional to the population in year n+1. If the populations in the years 1994, 1995, and 1997 were 39, 60, and 123, respectively, then the population in 1996 was
 - (A) 81
- **(B)** 84
- (C) 87
- **(D)** 90
- **(E)** 102
- 15. Medians BD and CE of triangle ABC are perpendicular, BD=8, and CE=12. The area of triangle ABC is
 - **(A)** 24
- **(B)** 32
- **(C)** 48
- **(D)** 64
- **(E)** 96



16. The three row sums and the three column sums of the array

$$\left[\begin{array}{ccc} 4 & 9 & 2 \\ 8 & 1 & 6 \\ 3 & 5 & 7 \end{array}\right]$$

are the same. What is the least number of entries that must be altered to make all six sums different from one another?

- **(A)** 1
- **(B)** 2
- **(C)** 3
- **(D)** 4
- **(E)** 5
- 17. A line x = k intersects the graph of $y = \log_5 x$ and the graph of $y = \log_5(x+4)$. The distance between the points of intersection is 0.5. Given that $k = a + \sqrt{b}$, where a and b are integers, what is a + b?
 - **(A)** 6
- **(B)** 7
- **(C)** 8
- **(D)** 9
- **(E)** 10
- 18. A list of integers has mode 32 and mean 22. The smallest number in the list is 10. The median m of the list is a member of the list. If the list member m were replaced by m + 10, the mean and median of the new list would be 24 and m + 10, respectively. If m were instead replaced by m 8, the median of the new list would be m 4. What is m?
 - **(A)** 16
- **(B)** 17
- **(C)** 18
- **(D)** 19
- **(E)** 20
- 19. A circle with center O is tangent to the coordinate axes and to the hypotenuse of the 30° - 60° - 90° triangle ABC as shown, where AB=1. To the nearest hundredth, what is the radius of the circle?
 - **(A)** 2.18
- **(B)** 2.24
- **(C)** 2.31
- **(D)** 2.37
- **(E)** 2.41

- 20. Which one of the following integers can be expressed as the sum of 100 consecutive positive integers?
 - (A) 1,627,384,950
- **(B)** 2,345,678,910
- (C) 3,579,111,300

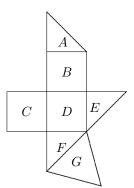
- **(D)** 4,692,581,470
- **(E)** 5,815,937,260
- 21. For any positive integer n, let

$$f(n) = \begin{cases} \log_8 n, & \text{if } \log_8 n \text{ is rational,} \\ 0, & \text{otherwise.} \end{cases}$$

What is $\sum_{n=1}^{1997} f(n)$?

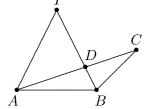
- **(A)** $\log_8 2047$ **(B)** 6 **(C)** $\frac{55}{3}$ **(D)** $\frac{58}{3}$ **(E)** 585

- 22. Ashley, Betty, Carlos, Dick, and Elgin went shopping. Each had a whole number of dollars to spend, and together they had \$56. The absolute difference between the amounts Ashley and Betty had to spend was \$19. The absolute difference between the amounts Betty and Carlos had was \$7, between Carlos and Dick was \$5, between Dick and Elgin was \$4, and between Elgin and Ashley was \$11. How much did Elgin have?
 - (A) \$6
- **(B)** \$7
- (C) \$8
- **(D)** \$9
- **(E)** \$10
- 23. In the figure, polygons A, E, and F are isosceles right triangles; B, C, and D are squares with sides of length 1; and G is an equilateral triangle. The figure can be folded along its edges to form a polyhedron having the polygons as faces. The volume of this polyhedron is



- (A) 1/2
- **(B)** 2/3
- (C) 3/4
- **(D)** 5/6
- **(E)** 4/3
- 24. A rising number, such as 34689, is a positive integer each digit of which is larger than each of the digits to its left. There are $\binom{9}{5} = 126$ five-digit rising numbers. When these numbers are arranged from smallest to largest, the 97th number in the list does not contain the digit
 - (A) 4
- **(B)** 5
- (C) 6
- (D) 7
- **(E)** 8

- 25. Let ABCD be a parallelogram and let $\overrightarrow{AA'}$, $\overrightarrow{BB'}$, $\overrightarrow{CC'}$, and $\overrightarrow{DD'}$ be parallel rays in space on the same side of the plane determined by ABCD. If AA' = 10, BB' = 8, CC' = 18, DD' = 22, and M and N are the midpoints of $\overrightarrow{A'C'}$ and $\overrightarrow{B'D'}$, respectively, then MN =
 - (A) 0 (B) 1 (C) 2 (D) 3 (E) 4
- 26. Triangle ABC and point P in the same plane are given. Point P is equidistant from A and B, angle APB is twice angle ACB, and \overline{AC} intersects \overline{BP} at point D. If PB=3 and PD=2, then $AD\cdot CD=$



- (A) 5 (B) 6 (C) 7 (D) 8 (E) 9
- 27. Consider those functions f that satisfy f(x+4) + f(x-4) = f(x) for all real x. Any such function is periodic, and there is a least common positive period p for all of them. Find p.
 - (A) 8 (B) 12 (C) 16 (D) 24 (E) 32
- 28. How many ordered triples of integers (a, b, c) satisfy

$$|a+b|+c=19$$
 and $ab+|c|=97$?

- (A) 0 (B) 4 (C) 6 (D) 10 (E) 12
- 29. Call a positive real number *special* if it has a decimal representation that consists entirely of digits 0 and 7. For example, $\frac{700}{99} = 7.\overline{07} = 7.070707...$ and 77.007 are special numbers. What is the smallest n such that 1 can be written as a sum of n special numbers?
 - **(A)** 7 **(B)** 8 **(C)** 9 **(D)** 10
 - (E) 1 cannot be represented as a sum of finitely many special numbers
- 30. For positive integers n, denote by D(n) the number of pairs of different adjacent digits in the binary (base two) representation of n. For example, $D(3) = D(11_2) = 0$, $D(21) = D(10101_2) = 4$, and $D(97) = D(1100001_2) = 2$. For how many positive integers n less than or equal to 97 does D(n) = 2?
 - (A) 16 (B) 20 (C) 26 (D) 30 (E) 35